

COMPUTER PROGRAM LISTING APPENDIX

COMPUTER PROGRAM LISTING APPENDIX

Votc.h

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/*
*****
* file:      tc_v2.h
* date:      April 12, 2000
* function:   tests turbo codes
*            Modulation: QAM
*            Decoder:  MAP algorithm
*****
*/

#include <math.h>
#include <stdio.h>
#include <malloc.h>
#include <dos.h>

/* Definition of the first recursive systematic code (RSC1): */
#define RSC1_ENC_MEM 4 /* encoder memory order */
#define RSC1_STATES (1 << RSC1_ENC_MEM)
#define RSC1_FP 035 /* forward polynomial in octal */
#define RSC1_BP 023 /* backward polynomial in octal */

/* Definition of the second recursive systematic code (RSC2): */
#define RSC2_ENC_MEM 4 /* encoder memory order */
#define RSC2_STATES (1 << RSC2_ENC_MEM)
#define RSC2_FP 035 /* forward polynomial in octal */
#define RSC2_BP 023 /* backward polynomial in octal */

#define NR_ITER 8 /* nr. of iterative decoding stages */
#define EBNO 6.0 /* Eb/No in dB */
#define MAX_ERRORS 1000 /* stop when this nr. is reached */
#define INT_SIZE 6144 /* nr. of info bits to be interleaved */

#define MAX (exp(31.0)) /* limit soft outputs */
#define E_STEPS 1000 /* number of values for E_val */
#define PRINT_BLOCKS 100 /* how often to print results */
#define SEED1 13733 /* seeds for random nr. gen. */
#define SEED2 1935791

#define SIGMA_12_4AM sqrt(2.50 * pow(10.0, (-EBNO / 10.0))) /* A = 1.0 */
#define SIGMA_12_16QAM sqrt(2.50 * pow(10.0, (-EBNO / 10.0)))
#define SIGMA_34_16QAM sqrt((10.0/6.0) * pow(10.0, (-EBNO / 10.0)))

/* For 8AM, 64QAM, 256QAM, A = 0.5 => A*A = 0.25. Thus, Eav = 5.25*A*A = Eav/4 */
#define SIGMA_56_64QAM sqrt(4.2/4 * pow(10.0, (-EBNO / 10.0)))
#define SIGMA_46_64QAM sqrt(5.25/4 * pow(10.0, (-EBNO / 10.0)))
#define SIGMA_23_8AM sqrt(5.25/4 * pow(10.0, (-EBNO / 10.0)))
#define SIGMA_12_8AM sqrt(7.0/4 * pow(10.0, (-EBNO / 10.0)))
#define SIGMA_58_256QAM sqrt(17.0/4 * pow(10.0, (-EBNO / 10.0)))
#define SIGMA_68_256QAM sqrt((170.0/12)/4 * pow(10.0, (-EBNO / 10.0)))

/* For 4QAM (A = 0.5): */
#define SIGMA_24_4QAM sqrt(2.0/2.0/4 * pow(10.0, (-EBNO / 10.0))) /* 1 info */
#define SIGMA_26_4QAM sqrt(2.0/(4.0/3)/4 * pow(10.0, (-EBNO / 10.0))) /* 2/3 info */
/* For 8QAM (A = 0.5): */
#define SIGMA_4AM_of_46_8QAM sqrt(6.0/4.0/4 * pow(10.0, (-EBNO / 10.0))) /* 2 info */
#define SIGMA_2AM_of_46_8QAM sqrt(6.0/4.0/4 * pow(10.0, (-EBNO / 10.0))) /* 2 info */
#define SIGMA_4AM_of_26_8QAM sqrt(6.0/2.0/4 * pow(10.0, (-EBNO / 10.0))) /* 1 info */
#define SIGMA_2AM_of_26_8QAM sqrt(6.0/2.0/4 * pow(10.0, (-EBNO / 10.0))) /* 1 info */
#define SIGMA_4AM_of_13_8QAM sqrt(6.0/2.0/4 * pow(10.0, (-EBNO / 10.0))) /* 1 info */
#define SIGMA_2AM_of_13_8QAM sqrt(6.0/2.0/4 * pow(10.0, (-EBNO / 10.0))) /* 1 info */
#define SIGMA_36_64QAM sqrt(42.0/6.0/4 * pow(10.0, (-EBNO / 10.0))) /* 3 info */

/* For 16QAM, 64QAM, 256QAM, 1024QAM (A = 0.5): */
#define SIGMA_412_16QAM sqrt(10.0/(8.0/3)/1 * pow(10.0, (-EBNO / 10.0))) /* 4/3 A=1 */
#define SIGMA_26_64QAM sqrt(42.0/4.0/4 * pow(10.0, (-EBNO / 10.0))) /* 2 info */
#define SIGMA_824_256QAM sqrt(170.0/(10.0/3)/4 * pow(10.0, (-EBNO / 10.0))) /* 10/3 */
#define SIGMA_1030_1024QAM sqrt(341.0/(10.0/3)/4 * pow(10.0, (-EBNO / 10.0))) /* 10/3 */

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/* For 32QAM, 128QAM, 512QAM, (A = 0.5):*/
#define SIGMA_8AM_of_115_32QAM sqrt(21.0/2/4 * pow(10.0, (-EBNO / 10.0))) /* 1 info */
#define SIGMA_4AM_of_115_32QAM sqrt(5.00/(4/3)/4 * pow(10.0, (-EBNO / 10.0))) /*2/3*/
#define SIGMA_16AM_of_721_128QAM sqrt(85.0/(8/3)/4 * pow(10.0, (-EBNO / 10.0))) /*4/3*/
#define SIGMA_8AM_of_721_128QAM sqrt(21.0/2/4 * pow(10.0, (-EBNO / 10.0))) /* 1 info */
#define SIGMA_32AM_of_39_512QAM sqrt(341.0/4/4*pow(10.0, (-EBNO / 10.0))) /* 2 info */
#define SIGMA_16AM_of_39_512QAM sqrt(85.00/2/4*pow(10.0, (-EBNO / 10.0))) /* 1 info */

/* For 32QAM (A = 0.5):*/
#define SIGMA_8AM_of_32QAM sqrt(26.0/6/4 * pow(10.0, (-EBNO / 10.0))) /* 3 info */
#define SIGMA_4AM_of_32QAM sqrt(26.0/6/4 * pow(10.0, (-EBNO / 10.0))) /* 3 info */

/* For R57_128QAM (A = 0.5):*/
#define SIGMA_16AM_of_128QAM sqrt(106.0/10/4 * pow(10.0, (-EBNO / 10.0))) /* 3 info */
#define SIGMA_8AM_of_128QAM sqrt(106.0/10/4 * pow(10.0, (-EBNO / 10.0))) /* 2 info */

/* For R69_512QAM (A = 0.5):*/
#define SIGMA_32AM_of_512QAM sqrt(426.0/12/4*pow(10.0, (-EBNO / 10.0))) /* 4 info */
#define SIGMA_16AM_of_512QAM sqrt(426.0/12/4*pow(10.0, (-EBNO / 10.0))) /* 2 info */

/* For R710_1024QAM (A = 0.5):*/
#define SIGMA_710_1024QAM sqrt((341.0/7)/4 * pow(10.0, (-EBNO / 10.0))) /* 3.5 info */

/* Define the particular coding and modulation case for simulation */
#define R36_64QAM

#define BIT_HIST
#define THRESHOLD_ITER 10 /* record bit histogram for higher iterations */
#define MAX_BIT_HIST_ARRAY (2 * INT_SIZE)
#define ERROR_FILE_NAME "../results/R36_64QAM_6144_test_30.err"
#define FRAME_HIST_FILE_NAME "../results/test.fhist"
#define BIT_HIST_FILE_NAME "../results/map.hist"
#define INTERLEAVER_FILE "../results/6144/s6144"

/*
* Note1:
Make sure that for each simulation, the INT_SIZE represents the size of the interleaver
defined in INTERLEAVER_FILE
*/

/*
* Note2:
In rate 4/6 64QAM_TTCM only two bits out of four are coded rate half. Therefore,
the first half of the interleaver table used has a INT_SIZE/2 interleaver,
the rest is mapping the bits in the same position.
*/

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Votc.c

```

/*
*****
* file:      tc_v2.c
* date:      March 20, 2000
* function:   tests turbo codes
*            Modulation: QAM
*            Decoder:  MAP algorithm
*****
*/

#include "tc_v2.h"

typedef struct {
    int      enc_state;          /* encoder state */
    int      nr_states;         /* number of encoder states */
    int      enc_mem;           /* encoder memory */
    int      bp;                /* backward polynomial */
    int      fp;                /* forward polynomial */
    int      *P0state;          /* previous state for i=0 branch */
    int      *P1state;          /* previous state for i=1 branch */
    int      *N0state;          /* next state for i=0 branch */
    int      *N1state;          /* next state for i=1 branch */
    int      *Coded0;           /* coded bit for i=0 branch */
    int      *Coded1;           /* coded bit for i=1 branch */
} jat_code;

void      jat_map1(jat_code *, double *, double *, double *, double *);
void      jat_map2(jat_code *, double *, double *, double *, double *);
void      jat_trellis_bp_fp(jat_code *);
int      jat_ps(jat_code *, int);
int      jat_enc_bp_fp(jat_code *, int);
void      r_ileav(double *, int *);
void      r_ileava(int *, int *);
void      r_deileav(double *, int *);
void      r_deileava(int *, int *);
double   nrngen();
int      nrngenbin();
double   gasdev();
int      errors(int *, double *, int, int);
int      print_err(int *, double *, int, int, int *);
double   find_tx_I(int);
double   find_tx_Q(int);

int      *frame_hist;          /* how many frames with how many errors*/
int      **bit_hist_array;     /* pointer to NR_ITER pointers
                                to blocks of data organised as:
                                block nr.,bit pos. in error,
                                block nr.,bit pos. in error */
int      *bit_hist_block;     /* current number of blocks in error
                                for each iteration */
int      frame_err;           /* frame/block error rate */
int      total_err;           /* total nr. of err. after NR_ITER */
long     s1, s2;              /* seed generators */

/*****
main()
{
    jat_code      *jat_code1;
    jat_code      *jat_code2;
    int      u1, u2, u3, u4, u5, u6;      /* bits of a 64QAM symbol in TTCM */
    double   tx_I, tx_Q, rx_I, rx_Q;
    double   v00_I, v00_Q, v01_I, v01_Q, v10_I, v10_Q, v11_I, v11_Q;
    int      i, j, k, block, iteration;
    int      *rule;                /* interleaver */
    int      *data;                /* the information block of data */

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int      *data_i;          /* the interleaved information block of data*/
int      *data_d;          /* the deinterleaved inf. block of data */
int      *Enc1;            /* Encoder1 output */
int      *Enc2;            /* Encoder2 output */
int      *no_err;          /* stores nr. err. for each iteration */
double   *D1_data;         /* Decoder1 input data */
double   *D1_parity;       /* Decoder1 input parity */
double   *D1_app;          /* Decoder1 input a priori information */
double   *D1_exi;          /* Decoder1 output extrinsic information */
double   *D2_data;         /* Decoder2 input data */
double   *D2_parity;       /* Decoder2 input parity */
double   *D2_app;          /* Decoder2 input a priori information */
double   *D2_exi;          /* Decoder2 output extrinsic information */
double   *Dec_data;        /* Decoded data */
double   *Zero_data;       /* zero data */
double   d0, d1, d2, d3, d4, L_d0, L_d1, L_d2, L_d3, tx, rx, K, noise1, n;
double   L_d4, L_d5;
double   L_u1, L_u2, L_u3, L_u4, L_u5, L_u6;
double   noise_I, noise_Q;
FILE      *out_file = NULL;

s1      = SEED1; /* initialize the seeds for the noise generator */
s2      = SEED2;
frame_err = 0;
total_err = 0;

/*
 * initialize the code structures:
 */
jat_code1 = (jat_code *)malloc(sizeof(jat_code));
jat_code1->enc_mem = RSC1_ENC_MEM;
jat_code1->bp = RSC1_BP;
jat_code1->fp = RSC1_FP;
jat_code1->enc_state = 0;
jat_code1->nr_states = (1 << RSC1_ENC_MEM);
jat_code1->P0state = (int *)malloc(sizeof(int)*jat_code1->nr_states);
jat_code1->P1state = (int *)malloc(sizeof(int)*jat_code1->nr_states);
jat_code1->N0state = (int *)malloc(sizeof(int)*jat_code1->nr_states);
jat_code1->N1state = (int *)malloc(sizeof(int)*jat_code1->nr_states);
jat_code1->Coded0 = (int *)malloc(sizeof(int)*jat_code1->nr_states);
jat_code1->Coded1 = (int *)malloc(sizeof(int)*jat_code1->nr_states);
jat_trellis_bp_fp(jat_code1);
jat_code2 = (jat_code *)malloc(sizeof(jat_code));
jat_code2->enc_mem = RSC2_ENC_MEM;
jat_code2->bp = RSC2_BP;
jat_code2->fp = RSC2_FP;
jat_code2->enc_state = 0;
jat_code2->nr_states = (1 << RSC2_ENC_MEM);
jat_code2->P0state = (int *)malloc(sizeof(int)*jat_code2->nr_states);
jat_code2->P1state = (int *)malloc(sizeof(int)*jat_code2->nr_states);
jat_code2->N0state = (int *)malloc(sizeof(int)*jat_code2->nr_states);
jat_code2->N1state = (int *)malloc(sizeof(int)*jat_code2->nr_states);
jat_code2->Coded0 = (int *)malloc(sizeof(int)*jat_code2->nr_states);
jat_code2->Coded1 = (int *)malloc(sizeof(int)*jat_code2->nr_states);
jat_trellis_bp_fp(jat_code2);

data = (int *)malloc(sizeof(int) * INT_SIZE);
if(data == 0)
{
    printf("Couldn't allocate data memory!\n");
    exit(1);
}

data_i = (int *)malloc(sizeof(int) * INT_SIZE);
if(data_i == 0)
{
    printf("Couldn't allocate data_i memory!\n");
    exit(1);
}

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data_d = (int *)malloc(sizeof(int) * INT_SIZE);
if(data_d == 0)
{
    printf("Couldn't allocate data_d memory!\n");
    exit(1);
}

no_err = (int *)malloc(sizeof(int) * NR_ITER);
if(no_err == 0)
{
    printf("Couldn't allocate no_err memory!\n");
    exit(1);
}
else
    for(i = 0; i < NR_ITER; i++)
        no_err[i] = 0;

Enc1 = (int *)malloc(sizeof(int) * INT_SIZE);
if(Enc1 == 0)
{
    printf("Couldn't allocate Enc1 memory!\n");
    exit(1);
}

Enc2 = (int *)malloc(sizeof(int) * INT_SIZE);
if(Enc2 == 0)
{
    printf("Couldn't allocate Enc2 memory!\n");
    exit(1);
}

D1_data = (double *)malloc(sizeof(double) * INT_SIZE);
if(D1_data == 0)
{
    printf("Couldn't allocate D1_data memory!\n");
    exit(1);
}

D1_parity = (double *)malloc(sizeof(double) * INT_SIZE);
if(D1_parity == 0)
{
    printf("Couldn't allocate D1_parity memory!\n");
    exit(1);
}

D1_app = (double *)malloc(sizeof(double) * INT_SIZE);
if(D1_app == 0)
{
    printf("Couldn't allocate D1_app memory!\n");
    exit(1);
}

D1_exi = (double *)malloc(sizeof(double) * INT_SIZE);
if(D1_exi == 0)
{
    printf("Couldn't allocate D1_exi memory!\n");
    exit(1);
}

D2_data = (double *)malloc(sizeof(double) * INT_SIZE);
if(D2_data == 0)
{
    printf("Couldn't allocate D2_data memory!\n");
    exit(1);
}

D2_parity = (double *)malloc(sizeof(double) * INT_SIZE);
if(D2_parity == 0)
{
    printf("Couldn't allocate D2_parity memory!\n");
    exit(1);
}

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    }

D2_app = (double *)malloc(sizeof(double) * INT_SIZE);
if(D2_app == 0)
{
    printf("Couldn't allocate D2_app memory!\n");
    exit(1);
}

D2_exi = (double *)malloc(sizeof(double) * INT_SIZE);
if(D2_exi == 0)
{
    printf("Couldn't allocate D2_exi memory!\n");
    exit(1);
}

Dec_data = (double *)malloc(sizeof(double) * INT_SIZE);
if(Dec_data == 0)
{
    printf("Couldn't allocate Dec_data memory!\n");
    exit(1);
}

Zero_data = (double *)malloc(sizeof(double) * INT_SIZE);
if(Zero_data == 0)
{
    printf("Couldn't allocate Zero_data memory!\n");
    exit(1);
}
for(i = 0; i < INT_SIZE; i++)
    Zero_data[i] = 0.0;

frame_hist = (int *)malloc(sizeof(int) * (INT_SIZE+1) * NR_ITER);
if(frame_hist == 0)
{
    printf("Couldn't allocate frame_hist memory!\n");
    exit(1);
}
else
{
    for(i = 0; i < (INT_SIZE+1)*NR_ITER; i++)
        frame_hist[i] = 0;
}

bit_hist_array = (int **)malloc(sizeof(int *) * 2 * NR_ITER);
if(bit_hist_array == 0)
{
    printf("Couldn't allocate bit_hist_array memory!\n");
    exit(1);
}
else
{
    for(i = THRESHOLD_ITER; i <= NR_ITER; i++)
    {
        bit_hist_array[i] = (int *)malloc(sizeof(int) * MAX_BIT_HIST_ARRAY);
        bit_hist_array[i+NR_ITER] = bit_hist_array[i]; /* store the original pointer */
        if(bit_hist_array[i] == 0)
        {
            printf("Couldn't allocate bit_hist_array[i] memory!\n");
            exit(1);
        }
    }
}

bit_hist_block = (int *)malloc(sizeof(int) * (NR_ITER+1));
if(bit_hist_block == 0)
{
    printf("Couldn't allocate bit_hist_block memory!\n");
    exit(1);
}
else

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    {
        for(i = 0; i <= NR_ITER; i++)
            bit_hist_block[i] = 1;
    }

rule = (int *)malloc(sizeof(int) * INT_SIZE * 2);
if(rule == 0)
{
    printf("Couldn't allocate rule memory!\n");
    exit(1);
}

for(i = 0; i < INT_SIZE; i++)
    rule[2*i] = 0;

/*
 * read the interleaver file
 */

out_file = fopen(INTERLEAVER_FILE, "r");

if(!out_file)
{
    printf("Error1: the output file could not be opened!\n");
    exit(1);
}

for(i = 0; i < INT_SIZE; i++)
    fscanf(out_file, "%d%d", &i, &rule[2*i+1]);
fclose(out_file);

/*
 * initialize the noise generator seeds in order to have the same data and
 * noise for different random interleavers
 */
s1 = SEED1;
s2 = SEED2;

/*
 * start the big loop:
 */
for(block = 1; total_err < MAX_ERRORS; block++)
{
    jat_code1->enc_state = 0;                /* reset encoder1's state */
    jat_code2->enc_state = 0;                /* reset encoder2's state */
    for(i = 0; i < INT_SIZE; i++)            /* no app for first decoder */
        D1_app[i] = 1.0;

    /*
     * generate random data:
     */
    for(i = 0; i < INT_SIZE; i++)
        data[i] = nrgenbin();

    /*
     * encoder1:
     */
    for(i = 0; i < INT_SIZE; i++)
        Enc1[i] = jat_enc_bp_fp(jat_code1, data[i]);

    /*
     * interleave data:
     */
    for(i = 0; i < INT_SIZE; i++)
        data_i[i] = data[i];
    r_ileava(data_i, rule);

    /*
     * encoder2:
     */
    for(i = 0; i < INT_SIZE; i++)

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    Enc2[i] = jat_enc_bp_fp(jat_code2, data_i[i]);

/*
 * deinterleave data:
 */
for(i = 0; i < INT_SIZE; i++)
    data_d[i] = data[i];
r_deileava(data_d, rule);

/*
 * modulate and add AWGN noise:
 */

#ifdef R12_4AM
/*
 * Channel:
 * d0 is MSB and d1 is LSB in a 4-AM: (d0,d1) = 01--00-|-10--11
 *                                     -3  -1   1   3
 */

n = (-1.0) / (2 * SIGMA_12_4AM * SIGMA_12_4AM);
for(i = 0; i < INT_SIZE; i++)
{
    d0 = data[i];
    if(i & 0x1)
        d1 = Enc1[i];
    else
        d1 = Enc2[i];
    tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
    rx = tx + SIGMA_12_4AM * gasdev();
    L_d0 = log((exp(n*(rx-1)*(rx-1))+exp(n*(rx-3)*(rx-3))) /
               (exp(n*(rx+1)*(rx+1))+exp(n*(rx+3)*(rx+3))));
    L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3))) /
               (exp(n*(rx-1)*(rx-1))+exp(n*(rx+1)*(rx+1))));
    D1_data[i] = L_d0;
    if(i & 0x1)
    {
        D1_parity[i] = L_d1;
        D2_parity[i] = 0.0;
    }
    else
    {
        D1_parity[i] = 0.0;
        D2_parity[i] = L_d1;
    }
}
#endif

#ifdef R13_8AM
/*
 * Channel:
 * d0 is MSB and d2 is LSB in 8-AM: (d0,d1,d2):
 *      010---011---001---000---100---101---111---110
 *      -3.5  -2.5  -1.5  -0.5   0.5   1.5   2.5   3.5
 */

n = (-1.0) / (2 * SIGMA_13_8AM * SIGMA_13_8AM);
for(i = 0; i < INT_SIZE; i++)
{
    d0 = data[i];
    if(i & 0x1)
    {
        d1 = Enc1[i];
        d2 = Enc2[i];
    }
    else
    {
        d1 = Enc2[i];
        d2 = Enc1[i];
    }
}

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    }

    tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
    rx = tx + SIGMA_13_8AM * gasdev();
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
        exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
        (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
        exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

    L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
        exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
        (exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
        exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

    L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
        exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
        (exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
        exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));

    D1_data[i] = L_d0;
    if(i & 0x1)
    {
        D1_parity[i] = L_d1;
        D2_parity[i] = L_d2;
    }
    else
    {
        D1_parity[i] = L_d2;
        D2_parity[i] = L_d1;
    }
}

#endif

#ifdef R12_8AM
/*
 * Channel:
 * d0 is MSB and d2 is LSB in 8-AM: (d0,d1,d2):
 *      010---011---001---000---100---101---111---110
 *      -3.5  -2.5  -1.5  -0.5   0.5   1.5   2.5   3.5
 */
/*
 * Channel: we transmit two 8AM symbols to emulate a 64QAM symbol.
 * 6 info bits and 6 parity bits are mapped to 2 64QAM symbols which in
 * turn are simulated as 4 8AM symbols to achieve 3bit/s/Hz
 *
 * INT_SIZE to be a multiple of 6
 */

n = (-1.0) / (2 * SIGMA_12_8AM * SIGMA_12_8AM);
for(i = 0; i < INT_SIZE; i++)
{
    /* symbol 1 */
    d0 = data[i];
    d1 = data[i+1];
    d2 = Enc1[i];
    tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
    rx = tx + SIGMA_12_8AM * gasdev();
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
        exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
        (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
        exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

    L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
        exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
        (exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
        exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

    L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
        exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
        (exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
        exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));
}

```

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```

D1_data[i]      = L_d0;
D1_data[i+1]    = L_d1;
D1_parity[i]    = L_d2;
D1_parity[i+1]  = 0;
D2_parity[i]    = 0;

/* symbol 2 */
d0 = data[i+2];
d1 = Enc1[i+2];
d2 = Enc2[i+1];
tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
rx = tx + SIGMA_12_8AM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
            exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
            (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
            exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
            exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
            (exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
            exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
            exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
            (exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
            exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));
D1_data[i+2]    = L_d0;
D1_parity[i+2]  = L_d1;
D2_parity[i+1]  = L_d2;
D2_parity[i+2]  = 0;

/* symbol 3 */
d0 = data[i+3];
d1 = data[i+4];
d2 = Enc2[i+3];
tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
rx = tx + SIGMA_12_8AM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
            exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
            (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
            exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
            exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
            (exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
            exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
            exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
            (exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
            exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));
D1_data[i+3]    = L_d0;
D1_data[i+4]    = L_d1;
D2_parity[i+3]  = L_d2;
D1_parity[i+3]  = 0;
D2_parity[i+4]  = 0;

/* symbol 4 */
d0 = data[i+5];
d1 = Enc1[i+4];
d2 = Enc2[i+5];
tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
rx = tx + SIGMA_12_8AM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
            exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
            (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
            exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
            exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
            (exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +

```

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```

exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)));

L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
(exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));
D1_data[i+5] = L_d0;
D1_parity[i+4] = L_d1;
D2_parity[i+5] = L_d2;
D1_parity[i+5] = 0;

i = i+5;
}
#endif

#ifdef R23_8AM
/*
* Channel:
* d0 is MSB and d2 is LSB in 8-AM: (d0,d1,d2):
* 010---011---001---000---100---101---111---110
* -3.5 -2.5 -1.5 -0.5 0.5 1.5 2.5 3.5
*/

n = (-1.0) / (2 * SIGMA_23_8AM * SIGMA_23_8AM);
for(i = 0; i < INT_SIZE; i++)
{
d0 = data[i];
d1 = data[i+1];
if(i & 0x4)
d2 = Enc1[i];
else
d2 = Enc2[i];

tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
rx = tx + SIGMA_23_8AM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
(exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));

D1_data[i] = L_d0;
D1_data[i+1] = L_d1;
if(i & 0x4)
{
D1_parity[i] = L_d2;
D1_parity[i+1] = 0;
D2_parity[i] = 0;
D2_parity[i+1] = 0;
}
else
{
D1_parity[i] = 0;
D1_parity[i+1] = 0;
D2_parity[i] = L_d2;
D2_parity[i+1] = 0;
}

i++;
}
#endif

```

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```

#ifdef R35_32QAM
/*
 * I dimension:
 * d0 is MSB and d2 is LSB in 8-AM: (d0,d1,d2):
 *   010---011---001---000---100---101---111---110
 *   -3.5  -2.5  -1.5  -0.5   0.5   1.5   2.5   3.5
 * Q dimension:
 * d0 is MSB and d1 is LSB in a 4-AM: (d0,d1):
 *   01----00----10----11
 *   -1.5  -0.5   0.5   1.5
 *
 * We transmit one 8AM symbol and one 4AM symbol to emulate a 32QAM symbol.
 * 6 info bits and 4 parity bits are mapped to 2 32QAM symbols.
 *
 * INT_SIZE to be a multiple of 6
 */

for(i = 0; i < INT_SIZE; i++)
{
    /* symbol 1: 8AM */
    d0 = data[i];
    d1 = data[i+2];
    d2 = Enc1[i];
    tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
    rx = tx + SIGMA_8AM_of_32QAM * gasdev();
    n = (-1.0) / (2 * SIGMA_8AM_of_32QAM * SIGMA_8AM_of_32QAM);
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

    L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

    L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
                (exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));

    D1_data[i] = L_d0;
    D1_data[i+2] = L_d1;
    D1_parity[i] = L_d2;
    D1_parity[i+1] = 0.0;
    D1_parity[i+2] = 0.0;
    D2_parity[i] = 0.0;
    D2_parity[i+2] = 0.0;

    /* symbol 2: 4AM */
    d0 = data[i+1];
    d1 = Enc2[i+1];
    tx = d0 - d1 + 2*d0*d1 - 0.5;
    rx = tx + SIGMA_4AM_of_32QAM * gasdev();
    n = (-1.0) / (2 * SIGMA_4AM_of_32QAM * SIGMA_4AM_of_32QAM);
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)))/
                (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5))));
    L_d1 = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5)*(rx-1.5)))/
                (exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx+0.5)*(rx+0.5))));
    D1_data[i+1] = L_d0;
    D2_parity[i+1] = L_d1;

    /* symbol 3: 8AM */
    d0 = data[i+3];
    d1 = data[i+5];
    d2 = Enc2[i+4];
    tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
    rx = tx + SIGMA_8AM_of_32QAM * gasdev();
    n = (-1.0) / (2 * SIGMA_8AM_of_32QAM * SIGMA_8AM_of_32QAM);
}

```

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L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
(exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));

D1_data[i+3] = L_d0;
D1_data[i+5] = L_d1;
D1_parity[i+4] = 0.0;
D1_parity[i+5] = 0.0;
D2_parity[i+3] = 0.0;
D2_parity[i+4] = L_d2;
D2_parity[i+5] = 0.0;

/* symbol 4: 4AM */
d0 = data[i+4];
d1 = Enc1[i+3];
tx = d0 - d1 + 2*d0*d1 - 0.5;
rx = tx + SIGMA_4AM_of_32QAM * gasdev();
n = (-1.0) / (2 * SIGMA_4AM_of_32QAM * SIGMA_4AM_of_32QAM);
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5))));
L_d1 = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5)*(rx-1.5)))/
(exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx+0.5)*(rx+0.5))));
D1_data[i+4] = L_d0;
D1_parity[i+3] = L_d1;

i = i+5;
}
#endif

#ifdef R46_64QAM_TTCM_VoCAL
/* Option 4
* Channel: I & Q defined as
*   -|-----|-----|-----|-----|-----|-----|
*   -3.5 -2.5 -1.5 -0.5 0.5 1.5 2.5 3.5
* the 64QAM symbol is defined as: (u1, u2, u3, u4, u5, u6)
* where u4 = d0
*         u3 = d1
*         u2 = p0 parity from ENC_H
*         u1 = q1 parity from ENC_V
*         u5 = d uncoded
*         u6 = d uncoded
* Use s4096v interleaver - only first 2048 bits are interleaved
*/

n = (-1.0) / (2 * SIGMA_46_64QAM * SIGMA_46_64QAM);
for(i = 0; i < INT_SIZE/2 -1;)
{
/* Encode only first half of INT_SIZE
* d0, d1, d2, d3,... up to INT_SIZE/2 - 1
* p0, 0, p2, 0,...
* 0, q1, 0, q3,...
*/
u4 = data[i];
u3 = data[i+1];
u2 = Enc1[i];
u1 = Enc2[i+1];
u5 = data[i+INT_SIZE/2];
u6 = data[i+INT_SIZE/2+1];

k = u6+2*u5+4*u4+8*u3+16*u2+32*u1;

```


Country	Year	Population (millions)	Urban population (millions)	Urban population (%)	Population density (per sq. km)	Urban population density (per sq. km)
Algeria	1970	10.0	4.0	40.0	100	400
Algeria	1975	11.0	4.5	40.9	110	450
Algeria	1980	12.0	5.0	41.7	120	500
Algeria	1985	13.0	5.5	42.3	130	550
Algeria	1990	14.0	6.0	42.9	140	600
Algeria	1995	15.0	6.5	43.3	150	650
Algeria	2000	16.0	7.0	43.8	160	700
Algeria	2005	17.0	7.5	44.1	170	750
Algeria	2010	18.0	8.0	44.4	180	800
Algeria	2015	19.0	8.5	44.7	190	850
Algeria	2020	20.0	9.0	45.0	200	900
Algeria	2025	21.0	9.5	45.2	210	950
Algeria	2030	22.0	10.0	45.5	220	1000
Algeria	2035	23.0	10.5	45.7	230	1050
Algeria	2040	24.0	11.0	45.8	240	1100
Algeria	2045	25.0	11.5	46.0	250	1150
Algeria	2050	26.0	12.0	46.2	260	1200
Algeria	2055	27.0	12.5	46.3	270	1250
Algeria	2060	28.0	13.0	46.4	280	1300
Algeria	2065	29.0	13.5	46.5	290	1350
Algeria	2070	30.0	14.0	46.7	300	1400
Algeria	2075	31.0	14.5	46.8	310	1450
Algeria	2080	32.0	15.0	46.9	320	1500
Algeria	2085	33.0	15.5	46.9	330	1550
Algeria	2090	34.0	16.0	47.1	340	1600
Algeria	2095	35.0	16.5	47.1	350	1650
Algeria	2100	36.0	17.0	47.2	360	1700
Algeria	2105	37.0	17.5	47.3	370	1750
Algeria	2110	38.0	18.0	47.4	380	1800
Algeria	2115	39.0	18.5	47.4	390	1850
Algeria	2120	40.0	19.0	47.5	400	1900
Algeria	2125	41.0	19.5	47.6	410	1950
Algeria	2130	42.0	20.0	47.6	420	2000
Algeria	2135	43.0	20.5	47.7	430	2050
Algeria	2140	44.0	21.0	47.7	440	2100
Algeria	2145	45.0	21.5	47.8	450	2150
Algeria	2150	46.0	22.0	47.8	460	2200
Algeria	2155	47.0	22.5	47.9	470	2250
Algeria	2160	48.0	23.0	47.9	480	2300
Algeria	2165	49.0	23.5	47.9	490	2350
Algeria	2170	50.0	24.0	48.0	500	2400
Algeria	2175	51.0	24.5	48.0	510	2450
Algeria	2180	52.0	25.0	48.1	520	2500
Algeria	2185	53.0	25.5	48.1	530	2550
Algeria	2190	54.0	26.0	48.1	540	2600
Algeria	2195	55.0	26.5	48.2	550	2650
Algeria	2200	56.0	27.0	48.2	560	2700
Algeria	2205	57.0	27.5	48.3	570	2750
Algeria	2210	58.0	28.0	48.3	580	2800
Algeria	2215	59.0	28.5	48.3	590	2850
Algeria	2220	60.0	29.0	48.3	600	2900
Algeria	2225	61.0	29.5	48.4	610	2950
Algeria	2230	62.0	30.0	48.4	620	3000
Algeria	2235	63.0	30.5	48.4		

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Year	1990	1991	1992	1993	1994	1995	1996	1997	1998	1999	2000	2001	2002	2003	2004	2005	2006	2007	2008	2009	2010	2011	2012	2013	2014	2015	2016	2017	2018	2019	2020	2021	2022	2023	2024	2025	2026	2027	2028	2029	2030	2031	2032	2033	2034	2035	2036	2037	2038	2039	2040	2041	2042	2043	2044	2045	2046	2047	2048	2049	2050	2051	2052	2053	2054	2055	2056	2057	2058	2059	2060	2061	2062	2063	2064	2065	2066	2067	2068	2069	2070	2071	2072	2073	2074	2075	2076	2077	2078	2079	2080	2081	2082	2083	2084	2085	2086	2087	2088	2089	2090	2091	2092	2093	2094	2095	2096	2097	2098	2099	2100
1990	1991	1992	1993	1994	1995	1996	1997	1998	1999	2000	2001	2002	2003	2004	2005	2006	2007	2008	2009	2010	2011	2012	2013	2014	2015	2016	2017	2018	2019	2020	2021	2022	2023	2024	2025	2026	2027	2028	2029	2030	2031	2032	2033	2034	2035	2036	2037	2038	2039	2040	2041	2042	2043	2044	2045	2046	2047	2048	2049	2050	2051	2052	2053	2054	2055	2056	2057	2058	2059	2060	2061	2062	2063	2064	2065	2066	2067	2068	2069	2070	2071	2072	2073	2074	2075	2076	2077	2078	2079	2080	2081	2082	2083	2084	2085	2086	2087	2088	2089	2090	2091	2092	2093	2094	2095	2096	2097	2098	2099	2100	

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```

exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q-0.5)*(rx_Q-0.5))) +
exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-0.5)*(rx_Q-0.5))) +
exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q-0.5)*(rx_Q-0.5))) +
exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q-0.5)*(rx_Q-0.5))) +
exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
(exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q+1.5)*(rx_Q+1.5))) +
exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q+1.5)*(rx_Q+1.5))) +
exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+1.5)*(rx_Q+1.5))) +
exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+1.5)*(rx_Q+1.5))) +
exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+1.5)*(rx_Q+1.5))) +
exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+1.5)*(rx_Q+1.5))) +
exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q+1.5)*(rx_Q+1.5))) +
exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q+1.5)*(rx_Q+1.5))) +
exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q+0.5)*(rx_Q+0.5)))));

```

```

D1_data[i]      = L_d3;
D1_data[i+1]    = L_d2;
D1_data[i + INT_SIZE/2] = rx_I;
D1_data[i + INT_SIZE/2 + 1] = rx_Q;
D1_parity[i]    = L_d1;
D1_parity[i+1]  = 0;
D2_parity[i]    = 0;
D2_parity[i+1]  = L_d0;

```

```

i = i + 2;

```

```

#endif

```

```

#ifdef R46_64QAM_TTCM_Ungerboeck_Map

```

```

/* Option3: conventional set partitioning used in TCM

```

```

* Channel: I & Q defined

```

```

*      -|-----|-----|-----|-----|-----|-----|-----|

```

COMPUTER PROGRAM LISTING APPENDIX

```

*      -3.5  -2.5  -1.5  -0.5   0.5   1.5   2.5   3.5
* the 64QAM symbol is defined as: (u1, u2, u3, u4, u5, u6)
* where
*      u6 = d0
*      u5 = d1
*      u4 = d2
*      u3 = d3
*      u2 = p0 parity from ENC_H
*      u1 = q1 parity from ENC_V
*/
/*
* deinterleave data:
*/
for(i = 0; i < INT_SIZE; i++)
    data_d[i] = data[i];
r_deileava(data_d, rule);
n_ = (-1.0) / (2 * SIGMA_46_64QAM * SIGMA_46_64QAM);
for(i = 0; i < INT_SIZE; i)
{
    /* Puncturing patern is:
    * d0, d1, d2, d3,...
    * p0, 0, 0, 0,...
    * 0, 0, q2, 0,...
    */

    u1 = Enc1[i];
    u2 = Enc2[i];
    u6 = data_d[i+3];
    u5 = data_d[i+2];
    u4 = data_d[i+1];
    u3 = data_d[i];

    k = u6+2*u5+4*u4+8*u3+16*u2+32*u1;

    tx_I = find_tx_I(k);
    tx_Q = find_tx_Q(k);

    rx_I = tx_I + SIGMA_46_64QAM * gasdev();
    rx_Q = tx_Q + SIGMA_46_64QAM * gasdev();

    L_d0 = log((exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
        exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
        exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
        exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
        exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
        exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
        exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
        exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
        exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
        exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
        exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
        exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
        exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q-0.5)*(rx_Q-0.5))) +
        exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q-0.5)*(rx_Q-0.5))) +
        exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-0.5)*(rx_Q-0.5))) +
        exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q-0.5)*(rx_Q-0.5))) +
        exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
        exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
        exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
        exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
        exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q+1.5)*(rx_Q+1.5))) +
        exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+1.5)*(rx_Q+1.5))) +
        exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+1.5)*(rx_Q+1.5))) +
        exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q+1.5)*(rx_Q+1.5))) +
        exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
        exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
        exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
        exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
        exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
        exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
        exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+3.5)*(rx_Q+3.5))) +

```

[illegible]

```

L_d1 = log((exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q+0.5)*(rx_Q+0.5))) +
exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q+2.5)*(rx_Q+2.5))) +
exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q+2.5)*(rx_Q+2.5)))) /
(exp(n*((rx_I+3.5)*(rx_I+3.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
exp(n*((rx_I+2.5)*(rx_I+2.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
exp(n*((rx_I+1.5)*(rx_I+1.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
exp(n*((rx_I+0.5)*(rx_I+0.5) + (rx_Q-2.5)*(rx_Q-2.5))) +
exp(n*((rx_I-0.5)*(rx_I-0.5) + (rx_Q-2.5)*(rx_Q-2.5))) +

```

COMPUTER PROGRAM LISTING A11

[illegible][illegible]

Country	Year	Population (millions)	Urban population (millions)	Urban population (%)	Population density (per sq km)	Urban population density (per sq km)
Algeria	1980	11.1	5.1	45.9	10.1	10.1
Algeria	1985	11.1	5.1	45.9	10.1	10.1
Algeria	1990	11.1	5.1	45.9	10.1	10.1
Algeria	1995	11.1	5.1	45.9	10.1	10.1
Algeria	2000	11.1	5.1	45.9	10.1	10.1
Algeria	2005	11.1	5.1	45.9	10.1	10.1
Algeria	2010	11.1	5.1	45.9	10.1	10.1
Algeria	2015	11.1	5.1	45.9	10.1	10.1
Algeria	2020	11.1	5.1	45.9	10.1	10.1
Algeria	2025	11.1	5.1	45.9	10.1	10.1
Algeria	2030	11.1	5.1	45.9	10.1	10.1
Algeria	2035	11.1	5.1	45.9	10.1	10.1
Algeria	2040	11.1	5.1	45.9	10.1	10.1
Algeria	2045	11.1	5.1	45.9	10.1	10.1
Algeria	2050	11.1	5.1	45.9	10.1	10.1
Algeria	2055	11.1	5.1	45.9	10.1	10.1
Algeria	2060	11.1	5.1	45.9	10.1	10.1
Algeria	2065	11.1	5.1	45.9	10.1	10.1
Algeria	2070	11.1	5.1	45.9	10.1	10.1
Algeria	2075	11.1	5.1	45.9	10.1	10.1
Algeria	2080	11.1	5.1	45.9	10.1	10.1
Algeria	2085	11.1	5.1	45.9	10.1	10.1
Algeria	2090	11.1	5.1	45.9	10.1	10.1
Algeria	2095	11.1	5.1	45.9	10.1	10.1
Algeria	2100	11.1	5.1	45.9	10.1	10.1
Algeria	2105	11.1	5.1	45.9	10.1	10.1
Algeria	2110	11.1	5.1	45.9	10.1	10.1
Algeria	2115	11.1	5.1	45.9	10.1	10.1
Algeria	2120	11.1	5.1	45.9	10.1	10.1
Algeria	2125	11.1	5.1	45.9	10.1	10.1
Algeria	2130	11.1	5.1	45.9	10.1	10.1
Algeria	2135	11.1	5.1	45.9	10.1	10.1
Algeria	2140	11.1	5.1	45.9	10.1	10.1
Algeria	2145	11.1	5.1	45.9	10.1	10.1
Algeria	2150	11.1	5.1	45.9	10.1	10.1
Algeria	2155	11.1	5.1	45.9	10.1	10.1
Algeria	2160	11.1	5.1	45.9	10.1	10.1
Algeria	2165	11.1	5.1	45.9	10.1	10.1
Algeria	2170	11.1	5.1	45.9	10.1	10.1
Algeria	2175	11.1	5.1	45.9	10.1	10.1
Algeria	2180	11.1	5.1	45.9	10.1	10.1
Algeria	2185	11.1	5.1	45.9	10.1	10.1
Algeria	2190	11.1	5.1	45.9	10.1	10.1
Algeria	2195	11.1	5.1	45.9	10.1	10.1
Algeria	2200	11.1	5.1	45.9	10.1	10.1
Algeria	2205	11.1	5.1	45.9	10.1	10.1
Algeria	2210	11.1	5.1	45.9	10.1	10.1
Algeria	2215	11.1	5.1	45.9	10.1	10.1
Algeria	2220	11.1	5.1	45.9	10.1	10.1
Algeria	2225	11.1	5.1	45.9	10.1	10.1
Algeria	2230	11.1	5.1	45.9	10.1	10.1
Algeria	2235	11.1	5.1	45.9	10.1	10.1
Algeria	2240	11.1	5.1	45.9	10.1	10.1
Algeria	2245	11.1</				

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COMPUTER PROGRAM LISTING APPENDIX

[illegible]

COMPUTER PROGRAM LISTING AFR

```
exp(n*(rx_I-3.5)*(rx_I-3.5) + (rx_Q-1.5)*(rx_Q-1.5))) +
exp(n*(rx_I+3.5)*(rx_I+3.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*(rx_I+2.5)*(rx_I+2.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*(rx_I+1.5)*(rx_I+1.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*(rx_I+0.5)*(rx_I+0.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*(rx_I-0.5)*(rx_I-0.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*(rx_I-1.5)*(rx_I-1.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*(rx_I-2.5)*(rx_I-2.5) + (rx_Q-3.5)*(rx_Q-3.5))) +
exp(n*(rx_I-3.5)*(rx_I-3.5) + (rx_Q-3.5)*(rx_Q-3.5))) );
```

[illegible]

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```

exp(n*((rx_I-1.5)*(rx_I-1.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
exp(n*((rx_I-2.5)*(rx_I-2.5) + (rx_Q+3.5)*(rx_Q+3.5))) +
exp(n*((rx_I-3.5)*(rx_I-3.5) + (rx_Q+3.5)*(rx_Q+3.5))));
D1_data[i] = L_d2;
D1_data[i+1] = L_d3;
D1_data[i+2] = L_d4;
D1_data[i+3] = L_d5;
D1_parity[i] = L_d0;
D1_parity[i+1] = 0.0;
D1_parity[i+2] = 0.0;
D1_parity[i+3] = 0.0;
D2_parity[i] = L_d1;
D2_parity[i+1] = 0.0;
D2_parity[i+2] = 0.0;
D2_parity[i+3] = 0.0;

i = i + 4;
}
/*
 * interleave data:
 */
r_ileav(D1_data, rule);

#endif

#ifdef R46_64QAM_IQ_Natural_Map
/* Option2
 * Channel: I = (u1, u2, u3), Q = (u4, u5, u6) defined using natural mapping:
 *      000  001  010  011  100  101  110  111
 *      -|-----|-----|-----|-----|-----|-----|-----|
 *      -3.5 -2.5 -1.5 -0.5  0.5  1.5  2.5  3.5
 * the 64QAM symbol is defined as: (u1, u2, u3, u4, u5, u6)
 * where:
 *      u1 = d0
 *      u2 = d1
 *      u3 = p0 parity from ENC_V
 *      u4 = d2
 *      u5 = d3
 *      u6 = q0 parity from ENC_H
 */

/*
 * deinterleave data:
 */
for(i = 0; i < INT_SIZE; i++)
    data_d[i] = data[i];
r_deileava(data_d, rule);

n = (-1.0) / (2 * SIGMA_46_64QAM * SIGMA_46_64QAM);

for(i = 0; i < INT_SIZE;)
{
    /* Puncturing pattern is:
     * d0, d1, d2, d3,...
     * p0, 0, 0, 0,...
     * q0, 0, 0, 0,...
     */

    u1 = data_d[i];
    u2 = data_d[i+1];
    u3 = Enc1[i];
    u4 = data_d[i+2];
    u5 = data_d[i+3];
    u6 = Enc2[i];

    tx_I = -3.5 + u3 + 2*u2 + 4*u1;
    tx_Q = -3.5 + u6 + 2*u5 + 4*u4;

    rx_I = tx_I + SIGMA_46_64QAM * gasdev();

```

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rx_Q = tx_Q + SIGMA_46_64QAM * gasdev();

L_u1 = log((exp(n*((rx_I-3.5)*(rx_I-3.5)))+
exp(n*((rx_I-2.5)*(rx_I-2.5)))+
exp(n*((rx_I-1.5)*(rx_I-1.5)))+
exp(n*((rx_I-0.5)*(rx_I-0.5))))/
(exp(n*((rx_I+3.5)*(rx_I+3.5)))+
exp(n*((rx_I+2.5)*(rx_I+2.5)))+
exp(n*((rx_I+1.5)*(rx_I+1.5)))+
exp(n*((rx_I+0.5)*(rx_I+0.5)))));
L_u2 = log((exp(n*((rx_I-3.5)*(rx_I-3.5)))+
exp(n*((rx_I-2.5)*(rx_I-2.5)))+
exp(n*((rx_I+1.5)*(rx_I+1.5)))+
exp(n*((rx_I+0.5)*(rx_I+0.5))))/
(exp(n*((rx_I+3.5)*(rx_I+3.5)))+
exp(n*((rx_I+2.5)*(rx_I+2.5)))+
exp(n*((rx_I-1.5)*(rx_I-1.5)))+
exp(n*((rx_I-0.5)*(rx_I-0.5)))));
L_u3 = log((exp(n*((rx_I-3.5)*(rx_I-3.5)))+
exp(n*((rx_I+2.5)*(rx_I+2.5)))+
exp(n*((rx_I-1.5)*(rx_I-1.5)))+
exp(n*((rx_I+0.5)*(rx_I+0.5))))/
(exp(n*((rx_I+3.5)*(rx_I+3.5)))+
exp(n*((rx_I-2.5)*(rx_I-2.5)))+
exp(n*((rx_I+1.5)*(rx_I+1.5)))+
exp(n*((rx_I-0.5)*(rx_I-0.5)))));

```

```

rx_I = rx_Q;

```

```

L_u4 = log((exp(n*((rx_I-3.5)*(rx_I-3.5)))+
exp(n*((rx_I-2.5)*(rx_I-2.5)))+
exp(n*((rx_I-1.5)*(rx_I-1.5)))+
exp(n*((rx_I-0.5)*(rx_I-0.5))))/
(exp(n*((rx_I+3.5)*(rx_I+3.5)))+
exp(n*((rx_I+2.5)*(rx_I+2.5)))+
exp(n*((rx_I+1.5)*(rx_I+1.5)))+
exp(n*((rx_I+0.5)*(rx_I+0.5)))));
L_u5 = log((exp(n*((rx_I-3.5)*(rx_I-3.5)))+
exp(n*((rx_I-2.5)*(rx_I-2.5)))+
exp(n*((rx_I+1.5)*(rx_I+1.5)))+
exp(n*((rx_I+0.5)*(rx_I+0.5))))/
(exp(n*((rx_I+3.5)*(rx_I+3.5)))+
exp(n*((rx_I+2.5)*(rx_I+2.5)))+
exp(n*((rx_I-1.5)*(rx_I-1.5)))+
exp(n*((rx_I-0.5)*(rx_I-0.5)))));
L_u6 = log((exp(n*((rx_I-3.5)*(rx_I-3.5)))+
exp(n*((rx_I+2.5)*(rx_I+2.5)))+
exp(n*((rx_I-1.5)*(rx_I-1.5)))+
exp(n*((rx_I+0.5)*(rx_I+0.5))))/
(exp(n*((rx_I+3.5)*(rx_I+3.5)))+
exp(n*((rx_I-2.5)*(rx_I-2.5)))+
exp(n*((rx_I+1.5)*(rx_I+1.5)))+
exp(n*((rx_I-0.5)*(rx_I-0.5)))));

```

```

D1_data[i] = L_u1;
D1_data[i+1] = L_u2;
D1_data[i+2] = L_u4;
D1_data[i+3] = L_u5;
D1_parity[i] = L_u3;
D1_parity[i+1] = 0.0;
D1_parity[i+2] = 0.0;
D1_parity[i+3] = 0.0;
D2_parity[i] = L_u6;
D2_parity[i+1] = 0.0;
D2_parity[i+2] = 0.0;
D2_parity[i+3] = 0.0;

```

```

i = i + 4;

```

```

/*
* interleave data:

```

```

    */
    r_ileav(Dl_data, rule);

#endif

#ifdef R46_64QAM_IO_Gray_Map
/* Option1: used in "Parallel Concatenated Trellis Coded Modulation" ICC'96
 * Channel: I = (u1, u2, u3), Q = (u4, u5, u6) defined using Gray mapping:
 * u1 & u4 are MSBs and u3 & u6 are LSBs:
 *      010---011---001---000---100---101---111---110
 *      -3.5  -2.5  -1.5  -0.5   0.5   1.5   2.5   3.5
 * where:
 *      u1 = d0
 *      u2 = d1
 *      u3 = p0 parity from ENC_V
 *      u4 = d2
 *      u5 = d3
 *      u6 = q0 parity from ENC_H
 *
 * INT_SIZE = multiple of 4
 */

n = (-1.0) / (2 * SIGMA_23_8AM * SIGMA_23_8AM);

/*
 * deinterleave data:
 */
for(i = 0; i < INT_SIZE; i++)
    data_d[i] = data[i];
r_deileava(data_d, rule);

for(i = 0; i < INT_SIZE;)
{
    /* Puncturing patern is:
     * d0, d1, d2, d3,...
     * p0, 0, 0, 0,...
     * q0, 0, 0, 0,...
     */

    u1 = data_d[i];
    u2 = data_d[i+1];
    u3 = Enc1[i];
    tx = 2*u1 - 2*u2 + 4*u1*u2 - 1.0 + (((2*u1-1)*(2*u2-1))<0?(u3-0.5):(0.5-u3));
    rx = tx + SIGMA_23_8AM * gasdev();
    L_u1 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

    L_u2 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

    L_u3 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
                (exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));

    u1 = data_d[i+2];
    u2 = data_d[i+3];
    u3 = Enc2[i];
    tx = 2*u1 - 2*u2 + 4*u1*u2 - 1.0 + (((2*u1-1)*(2*u2-1))<0?(u3-0.5):(0.5-u3));
    rx = tx + SIGMA_23_8AM * gasdev();
    L_u4 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

    L_u5 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +

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exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

L_u6 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
(exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));

D1_data[i]      = L_u1;
D1_data[i+1]    = L_u2;
D1_data[i+2]    = L_u4;
D1_data[i+3]    = L_u5;
D1_parity[i]    = L_u3;
D1_parity[i+1]  = 0.0;
D1_parity[i+2]  = 0.0;
D1_parity[i+3]  = 0.0;
D2_parity[i]    = L_u6;
D2_parity[i+1]  = 0.0;
D2_parity[i+2]  = 0.0;
D2_parity[i+3]  = 0.0;

i = i + 4;

}
/*
 * interleave data:
 */
r_ileav(D1_data, rule);

#endif

/*mio*/
#ifdef R24_4QAM
/*
 * Channel: we transmit two 2-AM symbols to emulate a 4-QAM symbol.
 * 2 info bits and 2 parity bits are mapped to 2 4-QAM symbols which in
 * turn are simulated as 4 2-AM symbols to achieve 1bit/s/Hz
 *
 * INT_SIZE to be a multiple of 2
 */
n = (-1.0) / (2 * SIGMA_24_4QAM * SIGMA_24_4QAM);
for(i = 0; i < INT_SIZE; i++)
{
    /* symbol 1 */
    d0 = data[i];
    tx = d0 - 0.5;
    rx = tx + SIGMA_24_4QAM * gasdev();
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5)) /
                (exp(n*(rx+0.5)*(rx+0.5))));
    D1_data[i] = L_d0;

    /* symbol 2 */
    d0 = Encl[i];
    tx = d0 - 0.5;
    rx = tx + SIGMA_24_4QAM * gasdev();
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5)) /
                (exp(n*(rx+0.5)*(rx+0.5))));
    D1_parity[i] = L_d0;

    /* symbol 3 */
    d0 = data[i+1];
    tx = d0 - 0.5;
    rx = tx + SIGMA_24_4QAM * gasdev();
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5)) /
                (exp(n*(rx+0.5)*(rx+0.5))));
    D1_data[i+1] = L_d0;

    /* symbol 4 */

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```

    d0 = Enc2[i+1];
    tx = d0 - 0.5;
    rx = tx + SIGMA_24_4QAM * gasdev();
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))) /
               (exp(n*(rx+0.5)*(rx+0.5))));
    D2_parity[i+1] = L_d0;
    D1_parity[i+1] = 0.0;
    D2_parity[i] = 0.0;
    i = i+1;
}
#endif

/*mio*/
#ifdef R26_4QAM
/*
 * Channel: we transmit two 2-AM symbols to emulate a 4-QAM symbol.
 * 2 info bits and 4 parity bits are mapped to 3 4-QAM symbols which in
 * turn are simulated as 6 2-AM symbols to achieve 1bit/s/Hz
 *
 * INT_SIZE to be a multiple of 2
 */
n = (-1.0) / (2 * SIGMA_26_4QAM * SIGMA_26_4QAM);
for(i = 0; i < INT_SIZE; i++)
{
    /* symbol 1 */
    d0 = data[i];
    tx = d0 - 0.5;
    rx = tx + SIGMA_26_4QAM * gasdev();
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))) /
               (exp(n*(rx+0.5)*(rx+0.5))));
    D1_data[i] = L_d0;

    /* symbol 2 */
    d0 = Enc1[i];
    tx = d0 - 0.5;
    rx = tx + SIGMA_26_4QAM * gasdev();
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))) /
               (exp(n*(rx+0.5)*(rx+0.5))));
    D1_parity[i] = L_d0;

    /* symbol 3 */
    d0 = Enc2[i];
    tx = d0 - 0.5;
    rx = tx + SIGMA_26_4QAM * gasdev();
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))) /
               (exp(n*(rx+0.5)*(rx+0.5))));
    D2_parity[i] = L_d0;

    /* symbol 4 */
    d0 = data[i+1];
    tx = d0 - 0.5;
    rx = tx + SIGMA_26_4QAM * gasdev();
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))) /
               (exp(n*(rx+0.5)*(rx+0.5))));
    D1_data[i+1] = L_d0;

    /* symbol 5 */
    d0 = Enc1[i+1];
    tx = d0 - 0.5;
    rx = tx + SIGMA_26_4QAM * gasdev();
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))) /
               (exp(n*(rx+0.5)*(rx+0.5))));
    D1_parity[i+1] = L_d0;

    /* symbol 6 */
    d0 = Enc2[i+1];
    tx = d0 - 0.5;
    rx = tx + SIGMA_26_4QAM * gasdev();
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))) /
               (exp(n*(rx+0.5)*(rx+0.5))));

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```

        D2_parity[i+1] = L_d0;
        i = i+1;
    }
#endif

/*mic*/
#ifdef R46_8QAM
/*
 * I dimension:
 * d0 is MSB and d1 is LSB in a 4-AM:(d0,d1):
 *      01----00----10----11
 *      -1.5  -0.5   0.5   1.5
 * Q dimension:
 * d0 is MSB in a 2-AM:(d0):
 *      0-----1
 *      -0.5   0.5
 *
 * We transmit one 4A-M symbol and one 2-AM symbol to emulate a 32QAM symbol.
 * 4 info bits and 2 parity bits are mapped to 2 8QAM symbols.
 *
 * INT_SIZE to be a multiple of 4
 */

for(i = 0; i < INT_SIZE; i++)
{
    /* symbol 1: 4AM */
    d0 = data[i];
    d1 = Enc1[i];
    tx  = d0 - d1 + 2*d0*d1 - 0.5;
    rx  = tx + SIGMA_4AM_of_46_8QAM * gasdev();
    n   = (-1.0) / (2 * SIGMA_4AM_of_46_8QAM * SIGMA_4AM_of_46_8QAM);
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))) /
               (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5))));
    L_d1 = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5)*(rx-1.5))) /
               (exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx+0.5)*(rx+0.5))));
    D1_data[i] = L_d0;
    D1_parity[i] = L_d1;

    /* symbol 2: 2AM */
    d0 = data[i+1];
    tx  = d0 - 0.5;
    rx  = tx + SIGMA_2AM_of_46_8QAM * gasdev();
    n   = (-1.0) / (2 * SIGMA_2AM_of_46_8QAM * SIGMA_2AM_of_46_8QAM);
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))) /
               (exp(n*(rx+0.5)*(rx+0.5))));
    D1_data[i+1] = L_d0;

    /* symbol 3: 4AM */
    d0 = data[i+2];
    d1 = Enc2[i+2];
    tx  = d0 - d1 + 2*d0*d1 - 0.5;
    rx  = tx + SIGMA_4AM_of_46_8QAM * gasdev();
    n   = (-1.0) / (2 * SIGMA_4AM_of_46_8QAM * SIGMA_4AM_of_46_8QAM);
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))) /
               (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5))));
    L_d1 = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5)*(rx-1.5))) /
               (exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx+0.5)*(rx+0.5))));
    D1_data[i+2] = L_d0;
    D2_parity[i+2] = L_d1;

    /* symbol 2: 4AM */
    d0 = data[i+3];
    tx  = d0 - 0.5;
    rx  = tx + SIGMA_2AM_of_46_8QAM * gasdev();
    n   = (-1.0) / (2 * SIGMA_2AM_of_46_8QAM * SIGMA_2AM_of_46_8QAM);
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))) /
               (exp(n*(rx+0.5)*(rx+0.5))));
    D1_data[i+3] = L_d0;
    D1_parity[i+1] = 0.0;
    D1_parity[i+2] = 0.0;
}

```

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```

D1_parity[i+3] = 0.0;
D2_parity[i] = 0.0;
D2_parity[i+1] = 0.0;
D2_parity[i+3] = 0.0;

    i = i+3;
}
#endif

/*mio*/
#ifdef R26_8QAM
/*
 * I dimension:
 * d0 is MSB and d1 is LSB in a 4-AM:(d0,d1):
 *      01----00----10----11
 *      -1.5  -0.5   0.5   1.5
 * Q dimension:
 * d0 is MSB in a 2-AM:(d0):
 *      0-----1
 *      -0.5   0.5
 *
 * We transmit one 4A-M symbol and one 2-AM symbol to emulate a 8QAM symbol.
 * 2 info bits and 4 parity bits are mapped to 2 8QAM symbols.
 *
 * INT_SIZE to be a multiple of 2
 */
for(i = 0; i < INT_SIZE; i++)
{
    /* symbol 1: 4AM */

    d0 = data[i];
    d1 = Enc1[i];
    tx = d0 - d1 + 2*d0*d1 - 0.5;
    rx = tx + SIGMA_4AM_of_26_8QAM * gasdev();
    n = (-1.0) / (2 * SIGMA_4AM_of_26_8QAM * SIGMA_4AM_of_26_8QAM);
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))) /
               (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5))));
    L_d1 = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5)*(rx-1.5))) /
               (exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx+0.5)*(rx+0.5))));
    D1_data[i] = L_d0;
    D1_parity[i] = L_d1;

    /* symbol 2: 2AM */

    d0 = Enc2[i];
    tx = d0 - 0.5;
    rx = tx + SIGMA_2AM_of_26_8QAM * gasdev();
    n = (-1.0) / (2 * SIGMA_2AM_of_26_8QAM * SIGMA_2AM_of_26_8QAM);
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))) /
               (exp(n*(rx+0.5)*(rx+0.5))));
    D2_parity[i] = L_d0;

    /* symbol 3: 4AM */

    d0 = Enc1[i+1];
    d1 = Enc2[i+1];
    tx = d0 - d1 + 2*d0*d1 - 0.5;
    rx = tx + SIGMA_4AM_of_26_8QAM * gasdev();
    n = (-1.0) / (2 * SIGMA_4AM_of_26_8QAM * SIGMA_4AM_of_26_8QAM);
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))) /
               (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5))));
    L_d1 = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5)*(rx-1.5))) /
               (exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx+0.5)*(rx+0.5))));
    D1_parity[i+1] = L_d0;
    D2_parity[i+1] = L_d1;

    /* symbol 4: 2AM */

    d0 = data[i+1];

```

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    tx  = d0 - 0.5;
    rx  = tx + SIGMA_2AM_of_26_8QAM * gasdev();
    n   = (-1.0) / (2 * SIGMA_2AM_of_26_8QAM * SIGMA_2AM_of_26_8QAM);
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))) /
               (exp(n*(rx+0.5)*(rx+0.5))));
    D1_data[i+1] = L_d0;
    i=i+1;
}

#endif

/*mio*/
#ifdef R13_8QAM
/*
 * I dimension:
 * d0 is MSB and d1 is LSB in a 4-AM:(d0,d1):
 *      01----00----10----11
 *      -1.5  -0.5   0.5   1.5
 * Q dimension:
 * d0 is MSB in a 2-AM:(d0):
 *      0-----1
 *      -0.5   0.5
 *
 * We transmit one 4A-M symbol and one 2-AM symbol to emulate a 8QAM symbol.
 * 1 info bits and 2 parity bits are mapped to 1 8QAM symbols.
 *
 * INT_SIZE to be a multiple of 1
 */

for(i = 0; i < INT_SIZE; i++)
{
    /* symbol 1: 4AM */

    d0 = data[i];
    d1 = Enc1[i];
    tx  = d0 - d1 + 2*d0*d1 - 0.5;
    rx  = tx + SIGMA_4AM_of_13_8QAM * gasdev();
    n   = (-1.0) / (2 * SIGMA_4AM_of_13_8QAM * SIGMA_4AM_of_13_8QAM);
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))) /
               (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5))));
    L_d1 = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5)*(rx-1.5))) /
               (exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx+0.5)*(rx+0.5))));
    D1_data[i] = L_d0;
    D1_parity[i] = L_d1;

    /* symbol 2: 2AM */

    d0 = Enc2[i];
    tx  = d0 - 0.5;
    rx  = tx + SIGMA_2AM_of_13_8QAM * gasdev();
    n   = (-1.0) / (2 * SIGMA_2AM_of_13_8QAM * SIGMA_2AM_of_13_8QAM);
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))) /
               (exp(n*(rx+0.5)*(rx+0.5))));
    D2_parity[i] = L_d0;

}

#endif

/*mio*/
#ifdef R412_16QAM
/*
 * Channel: we transmit two 4-AM symbols to emulate a 16-QAM symbol.
 * 4 info bits and 8 parity bits are mapped to 3 16-QAM symbols which in
 * turn are simulated as 6 4-AM symbols to achieve 3bit/s/Hz
 * d0 is MSB and d1 is LSB in a 4-AM:(d0,d1) = 01----00--|--10----11
 *      -1.5  -0.5   0.5   1.5
 *
 * INT_SIZE to be a multiple of 4
 */

n = (-1.0) / (2 * SIGMA_412_16QAM * SIGMA_412_16QAM);
for(i = 0; i < INT_SIZE; i++)

```


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```

/* symbol 1 */
d0 = data[i];
d1 = Encl[i];
tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
rx = tx + SIGMA_412_16QAM * gasdev();
L_d0 = log((exp(n*(rx-1)*(rx-1))+exp(n*(rx-3)*(rx-3))) /
            (exp(n*(rx+1)*(rx+1))+exp(n*(rx+3)*(rx+3))));
L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3))) /
            (exp(n*(rx-1)*(rx-1))+exp(n*(rx+1)*(rx+1))));
D1_data[i] = L_d0;
D1_parity[i] = L_d1;

/* symbol 2 */
d0 = data[i+1];
d1 = Encl[i+1];
tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
rx = tx + SIGMA_412_16QAM * gasdev();
L_d0 = log((exp(n*(rx-1)*(rx-1))+exp(n*(rx-3)*(rx-3))) /
            (exp(n*(rx+1)*(rx+1))+exp(n*(rx+3)*(rx+3))));
L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3))) /
            (exp(n*(rx-1)*(rx-1))+exp(n*(rx+1)*(rx+1))));
D1_data[i+1] = L_d0;
D1_parity[i+1] = L_d1;

/* symbol 3 */
d0 = Enc2[i];
d1 = Enc2[i+1];
tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
rx = tx + SIGMA_412_16QAM * gasdev();
L_d0 = log((exp(n*(rx-1)*(rx-1))+exp(n*(rx-3)*(rx-3))) /
            (exp(n*(rx+1)*(rx+1))+exp(n*(rx+3)*(rx+3))));
L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3))) /
            (exp(n*(rx-1)*(rx-1))+exp(n*(rx+1)*(rx+1))));
D2_parity[i] = L_d0;
D2_parity[i+1] = L_d1;

/* symbol 4 */
d0 = data[i+2];
d1 = Encl[i+2];
tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
rx = tx + SIGMA_412_16QAM * gasdev();
L_d0 = log((exp(n*(rx-1)*(rx-1))+exp(n*(rx-3)*(rx-3))) /
            (exp(n*(rx+1)*(rx+1))+exp(n*(rx+3)*(rx+3))));
L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3))) /
            (exp(n*(rx-1)*(rx-1))+exp(n*(rx+1)*(rx+1))));
D1_data[i+2] = L_d0;
D1_parity[i+2] = L_d1;

/* symbol 5 */
d0 = Enc2[i+2];
d1 = Enc2[i+3];
tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
rx = tx + SIGMA_412_16QAM * gasdev();
L_d0 = log((exp(n*(rx-1)*(rx-1))+exp(n*(rx-3)*(rx-3))) /
            (exp(n*(rx+1)*(rx+1))+exp(n*(rx+3)*(rx+3))));
L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3))) /
            (exp(n*(rx-1)*(rx-1))+exp(n*(rx+1)*(rx+1))));
D2_parity[i+2] = L_d0;
D2_parity[i+3] = L_d1;

/* symbol 6 */
d0 = data[i+3];
d1 = Encl[i+3];
tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
rx = tx + SIGMA_412_16QAM * gasdev();
L_d0 = log((exp(n*(rx-1)*(rx-1))+exp(n*(rx-3)*(rx-3))) /
            (exp(n*(rx+1)*(rx+1))+exp(n*(rx+3)*(rx+3))));
L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3))) /
            (exp(n*(rx-1)*(rx-1))+exp(n*(rx+1)*(rx+1))));
D1_data[i+3] = L_d0;

```

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```

D1_parity[i+3] = L_d1;

        i = i+3;
    }
#endif

/*mio*/
#ifdef R515_32QAM
/*
 * I dimension:
 * d0 is MSB and d2 is LSB in 8-AM: (d0,d1,d2):
 *      010---011---001---000---100---101---111---110
 *      -3.5  -2.5  -1.5  -0.5   0.5   1.5   2.5   3.5
 * Q dimension:
 * d0 is MSB and d1 is LSB in a 4-AM: (d0,d1):
 *      01-----00-----10-----11
 *      -1.5  -0.5   0.5   1.5
 *
 * We transmit one 8AM symbol and one 4AM symbol to emulate a 32QAM symbol.
 * 5 info bits and 10 parity bits are mapped to 3 32QAM symbols.
 *
 * INT_SIZE to be a multiple of 5
 */

for(i = 0; i < INT_SIZE; i++)
{
    /* symbol 1: 8AM */
    d0 = data[i];
    d1 = Enc1[i];
    d2 = Enc2[i];
    tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
    rx = tx + SIGMA_8AM_of_515_32QAM * gasdev();
    n = (-1.0) / (2 * SIGMA_8AM_of_515_32QAM * SIGMA_8AM_of_515_32QAM);
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

    L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

    L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
                (exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));
    D1_data[i] = L_d0;
    D1_parity[i] = L_d1;
    D2_parity[i] = L_d2;

    /* symbol 2: 4AM */
    d0 = data[i+1];
    d1 = Enc1[i+1];
    tx = d0 - d1 + 2*d0*d1 - 0.5;
    rx = tx + SIGMA_4AM_of_515_32QAM * gasdev();
    n = (-1.0) / (2 * SIGMA_4AM_of_515_32QAM * SIGMA_4AM_of_515_32QAM);
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)))/
                (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5))));
    L_d1 = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5)*(rx-1.5)))/
                (exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx+0.5)*(rx+0.5))));
    D1_data[i+1] = L_d0;
    D2_parity[i+1] = L_d1;

    /* symbol 3: 8AM */
    d0 = data[i+2];
    d1 = Enc1[i+2];
    d2 = Enc2[i+2];
    tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
    rx = tx + SIGMA_8AM_of_515_32QAM * gasdev();

```

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```

n = (-1.0) / (2 * SIGMA_8AM_of_515_32QAM * SIGMA_8AM_of_515_32QAM);
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
(exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));
D1_data[i+2] = L_d0;
D1_parity[i+2] = L_d1;
D2_parity[i+1] = L_d2;

/* symbol 4: 4AM */
d0 = data[i+3];
d1 = Enc2[i+2];
tx = d0 - d1 + 2*d0*d1 - 0.5;
rx = tx + SIGMA_4AM_of_515_32QAM * gasdev();
n = (-1.0) / (2 * SIGMA_4AM_of_515_32QAM * SIGMA_4AM_of_515_32QAM);
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5))));
L_d1 = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5)*(rx-1.5)))/
(exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx+0.5)*(rx+0.5))));
D1_data[i+3] = L_d0;
D2_parity[i+2] = L_d1;

/* symbol 5: 8AM */
d0 = data[i+4];
d1 = Enc1[i+3];
d2 = Enc2[i+3];
tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
rx = tx + SIGMA_8AM_of_515_32QAM * gasdev();
n = (-1.0) / (2 * SIGMA_8AM_of_515_32QAM * SIGMA_8AM_of_515_32QAM);
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
(exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));
D1_data[i+4] = L_d0;
D1_parity[i+3] = L_d1;
D2_parity[i+3] = L_d2;

/* symbol 4: 4AM */
d0 = Enc1[i+4];
d1 = Enc2[i+4];
tx = d0 - d1 + 2*d0*d1 - 0.5;
rx = tx + SIGMA_4AM_of_515_32QAM * gasdev();
n = (-1.0) / (2 * SIGMA_4AM_of_515_32QAM * SIGMA_4AM_of_515_32QAM);
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5))));
L_d1 = log((exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx-1.5)*(rx-1.5)))/
(exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx+0.5)*(rx+0.5))));
D1_parity[i+4] = L_d0;
D2_parity[i+4] = L_d1;

i = i+4;

```

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```

    }
#endif

/*mio*/
#ifdef R26_64QAM
/*
 * Channel:
 * d0 is MSB and d2 is LSB in 8AM:(d0,d1,d2):
 *      010---011---001---000---100---101---111---110
 *      -3.5  -2.5  -1.5  -0.5   0.5   1.5   2.5   3.5
 */
/*
 * Channel: we transmit two 8AM symbols to emulate a 64QAM symbol.
 * 2 info bits and 4 parity bits are mapped to 1 64QAM symbols which in
 * turn are simulated as 2 8AM symbols to achieve 2bit/s/Hz.
 *
 * INT_SIZE to be a multiple of 2
 */
n = (-1.0) / (2 * SIGMA_26_64QAM * SIGMA_26_64QAM);
for(i = 0; i < INT_SIZE; i++)
{
/* symbol 1 */

    d0 = data[i];
    d1 = Enc1[i];
    d2 = Enc2[i];
    tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
    rx = tx + SIGMA_26_64QAM * gasdev();
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

    L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

    L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
                (exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));
    D1_data[i] = L_d0;
    D1_parity[i] = L_d1;
    D2_parity[i] = L_d2;

/* symbol 2 */

    d0 = data[i+1];
    d1 = Enc1[i+1];
    d2 = Enc2[i+1];
    tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
    rx = tx + SIGMA_26_64QAM * gasdev();
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

    L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

    L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
                (exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));
    D1_data[i+1] = L_d0;
    D1_parity[i+1] = L_d1;
    D2_parity[i+1] = L_d2;
    i = i+1;
}
}

```

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```

    }
#endif

/*mio*/
#ifdef R36_64QAM
/*
 * Channel:
 * d0 is MSB and d2 is LSB in 8AM:(d0,d1,d2):
 *      010---011---001---000---100---101---111---110
 *      -3.5  -2.5  -1.5  -0.5   0.5   1.5   2.5   3.5
 */
/*
 * Channel: we transmit two 8AM symbols to emulate a 64QAM symbol.
 * 6 info bits and 6 parity bits are mapped to 2 64QAM symbols which in
 * turn are simulated as 4 8AM symbols to achieve 2bit/s/Hz.
 *
 * INT_SIZE to be a multiple of 6
 */
n = (-1.0) / (2 * SIGMA_36_64QAM * SIGMA_36_64QAM);
for(i = 0; i < INT_SIZE; i++)
{
/* symbol 1 */

    d0 = data[i];
    d1 = data[i+1];
    d2 = Enc1[i];
    tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
    rx = tx + SIGMA_36_64QAM * gasdev();
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

    L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

    L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
                (exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));

    D1_data[i] = L_d0;
    D1_data[i+1] = L_d1;
    D1_parity[i] = L_d2;

/* symbol 2 */

    d0 = data[i+2];
    d1 = Enc1[i+2];
    d2 = Enc2[i+1];
    tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
    rx = tx + SIGMA_36_64QAM * gasdev();
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

    L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

    L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
                (exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));

    D1_data[i+2] = L_d0;
    D1_parity[i+2] = L_d1;
    D2_parity[i+1] = L_d2;
}
}

```

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/* symbol 3 */

d0 = data[i+3];
d1 = data[i+4];
d2 = Enc2[i+3];
tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
rx = tx + SIGMA_36_64QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
(exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));
D1_data[i+3] = L_d0;
D1_data[i+4] = L_d1;
D2_parity[i+3] = L_d2;

/* symbol 2 */

d0 = data[i+5];
d1 = Enc1[i+4];
d2 = Enc2[i+5];
tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
rx = tx + SIGMA_36_64QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
(exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));
D1_data[i+5] = L_d0;
D1_parity[i+4] = L_d1;
D2_parity[i+5] = L_d2;
D2_parity[i] = 0.0;
D1_parity[i+1] = 0.0;
D2_parity[i+2] = 0.0;
D1_parity[i+3] = 0.0;
D2_parity[i+4] = 0.0;
D1_parity[i+5] = 0.0;
i = i+5;
}
#endif

/*mio*/
#ifdef R721_128QAM
/*
* Q dimension:
* d0 is MSB and d2 is LSB in 8-AM: (d0,d1,d2):
* 010---011---001---000---100---101---111---110
* -3.5 -2.5 -1.5 -0.5 0.5 1.5 2.5 3.5
* I dimension:
* d0 is MSB and d3 is LSB in 16AM: (d0,d1,d2,d3):
*
* 0010---0011---0001---0000---0100---0101---0111---0110
* -7.5 -6.5 -5.5 -4.5 -3.5 -2.5 -1.5 -0.5
*/

```

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*
*      1010---1011---1001---1000---1100---1101---1111---1110
*      7.5    6.5    5.5    4.5    3.5    2.5    1.5    0.5
*
* INT_SIZE to be a multiple of 7
*/

for(i = 0; i < INT_SIZE; i++)
{
    /* symbol 1 Q dimension: 8AM */

    d0 = data[i+2];
    d1 = Enc1[i+1];
    d2 = Enc2[i+1];
    tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
    rx = tx + SIGMA_8AM_of_721_128QAM * gasdev();
    n = (-1.0) / (2 * SIGMA_8AM_of_721_128QAM * SIGMA_8AM_of_721_128QAM);
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

    L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

    L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
                (exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));
    D1_data[i+2] = L_d0;
    D1_parity[i+1] = L_d1;
    D2_parity[i+1] = L_d2;

    /* symbol 2 I dimension: 16AM */

    d0 = data[i];
    d1 = data[i+1];
    d2 = Enc1[i];
    d3 = Enc2[i];
    tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
    tx = (d0 == 0 ? (tx - 4) : (4 - tx));
    rx = tx + SIGMA_16AM_of_721_128QAM * gasdev();
    n = (-1.0) / (2 * SIGMA_16AM_of_721_128QAM * SIGMA_16AM_of_721_128QAM);
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
                exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
                exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
                (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
                exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
                exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

    L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
                exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
                exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
                exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

    L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
                exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
                (exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
                exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +

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exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)));

L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
(exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-7.5)*(rx-7.5))));

D1_data[i] = L_d0;
D1_data[i+1] = L_d1;
D1_parity[i] = L_d2;
D2_parity[i] = L_d3;

/* symbol 3 Q dimension: 8AM */

d0 = data[i+4];
d1 = Enc1[i+4];
d2 = Enc2[i+3];
tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
rx = tx + SIGMA_8AM_of_721_128QAM * gasdev();
n = (-1.0) / (2 * SIGMA_8AM_of_721_128QAM * SIGMA_8AM_of_721_128QAM);
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
(exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));
D1_data[i+4] = L_d0;
D1_parity[i+4] = L_d1;
D2_parity[i+3] = L_d2;

/* symbol 4 I dimension: 16AM */

d0 = data[i+3];
d1 = Enc1[i+3];
d2 = Enc1[i+2];
d3 = Enc2[i+2];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4) : (4 - tx));
rx = tx + SIGMA_16AM_of_721_128QAM * gasdev();
n = (-1.0) / (2 * SIGMA_16AM_of_721_128QAM * SIGMA_16AM_of_721_128QAM);
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +

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exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)));

L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
(exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-7.5)*(rx-7.5))));

D1_data[i+3]      = L_d0;
D1_parity[i+3]    = L_d1;
D1_parity[i+2]    = L_d2;
D2_parity[i+2]    = L_d3;

/* symbol 5 Q dimension: 8AM */

d0 = data[i+6];
d1 = Enc1[i+6];
d2 = Enc2[i+6];
tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
rx = tx + SIGMA_8AM_of_721_128QAM * gasdev();
n = (-1.0) / (2 * SIGMA_8AM_of_721_128QAM * SIGMA_8AM_of_721_128QAM);
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
(exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));
D1_data[i+6]      = L_d0;
D1_parity[i+6]    = L_d1;
D2_parity[i+6]    = L_d2;

/* symbol 6 I dimension: 16AM */

d0 = data[i+5];
d1 = Enc1[i+5];
d2 = Enc2[i+5];
d3 = Enc2[i+4];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4) : (4 - tx));
rx = tx + SIGMA_16AM_of_721_128QAM * gasdev();
n = (-1.0) / (2 * SIGMA_16AM_of_721_128QAM * SIGMA_16AM_of_721_128QAM);
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/

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        (exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
        exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
        exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
        exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)));

    L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
    exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
    exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
    exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
    (exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
    exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
    exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
    exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5))));

    L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
    exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+2.5)*(rx+2.5)) +
    exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
    exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
    (exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+4.5)*(rx+4.5)) +
    exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
    exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5)) +
    exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-7.5)*(rx-7.5))));

    D1_data[i+5]      = L_d0;
    D1_parity[i+5]    = L_d1;
    D2_parity[i+5]    = L_d2;
    D2_parity[i+4]    = L_d3;
    i = i+6;
}
#endif

/*mio*/
#ifdef R824_256QAM
/*
 * Channel:
 * d0 is MSB and d3 is LSB in 16AM: (d0,d1,d2,d3):
 *
 *      0010---0011---0001---0000---0100---0101---0111---0110
 *      -7.5   -6.5   -5.5   -4.5   -3.5   -2.5   -1.5   -0.5
 *
 *      1010---1011---1001---1000---1100---1101---1111---1110
 *      7.5     6.5     5.5     4.5     3.5     2.5     1.5     0.5
 *
 * Channel: we transmit two 16AM symbols to emulate a 256QAM symbol.
 * 8 info bits and 16 parity bits are mapped to 3 256QAM symbols which in
 * turn are simulated as 6 16AM symbols to achieve 8/3bit/s/Hz.
 *
 * INT_SIZE to be a multiple of 8
 */

n = (-1.0) / (2 * SIGMA_824_256QAM * SIGMA_824_256QAM);

/*
 * deinterleave data:
 */
for(i = 0; i < INT_SIZE; i++)
    data_d[i] = data[i];
r_deileava(data_d, rule);

for(i = 0; i < INT_SIZE; i++)
{
    /* symbol 1 */
    d0 = data_d[i];
    d1 = data_d[i+1];
    d2 = Enc1[i];
    d3 = Enc2[i];
    tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
    tx = (d0 == 0 ? (tx - 4) : (4 - tx));
    /* Test the mapping to the 16AM constellation:
     * if (i < 500)
    */
}

```

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* printf("\n(%d%d%d) = %f", (int)d0, (int)d1, (int)d2, (int)d3, tx);
*/
rx = tx + SIGMA_58_256QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5))));

L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
(exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-7.5)*(rx-7.5))));

D1_data[i] = L_d0;
D1_data[i+1] = L_d1;
D1_parity[i] = L_d2;
D2_parity[i] = L_d3;

/* symbol 2 */
d0 = data_d[i+2];
d1 = Encl[i+2];
d2 = Encl[i+1];
d3 = Encl[i+1];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4) : (4 - tx));
rx = tx + SIGMA_824_256QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +

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exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)));

L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
(exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-7.5)*(rx-7.5))));

D1_data[i+2] = L_d0;
D1_parity[i+2] = L_d1;
D1_parity[i+1] = L_d2;
D2_parity[i+1] = L_d3;

/* symbol 3 */
d0 = data_d[i+3];
d1 = Enc1[i+3];
d2 = Enc2[i+3];
d3 = Enc1[i+2];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4) : (4 - tx));
rx = tx + SIGMA 824_256QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5))));

L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
(exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-7.5)*(rx-7.5))));

D1_data[i+3] = L_d0;
D1_parity[i+3] = L_d1;
D2_parity[i+3] = L_d2;
D2_parity[i+2] = L_d3;

/* symbol 4 */
d0 = data_d[i+4];

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d1 = data_d[i+5];
d2 = Enc1[i+4];
d3 = Enc2[i+4];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4) : (4 - tx));
rx = tx + SIGMA_824_256QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5))));

L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
(exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-7.5)*(rx-7.5))));
D1_data[i+4] = L_d0;
D1_data[i+5] = L_d1;
D1_parity[i+4] = L_d2;
D2_parity[i+4] = L_d3;

/* symbol 5 */

d0 = data_d[i+6];
d1 = Enc1[i+6];
d2 = Enc1[i+5];
d3 = Enc2[i+5];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4) : (4 - tx));
rx = tx + SIGMA_824_256QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +

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```

exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)));

L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5))));

L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
(exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-7.5)*(rx-7.5))));

D1_data[i+6] = L_d0;
D1_parity[i+6] = L_d1;
D1_parity[i+5] = L_d2;
D2_parity[i+5] = L_d3;

/* symbol 4 */
d0 = data_d[i+7];
d1 = Enc1[i+7];
d2 = Enc2[i+7];
d3 = Enc2[i+6];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4) : (4 - tx));
rx = tx + SIGMA_824_256QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5))));

L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
(exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-7.5)*(rx-7.5))));

D1_data[i+7] = L_d0;
D1_parity[i+7] = L_d1;
D2_parity[i+7] = L_d2;
D2_parity[i+6] = L_d3;

```

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```

        i = i+7;
    }
    /*
     * interleave data:
     */
    r_ileav(D1_data, rule);
#endif

/*mio*/

#ifdef R69_512QAM
/*
 * Interleaver should be a multiple of 3, e.g., 6144
 *
 * Q dimension:
 * d0 is MSB and d4 is LSB in 32AM: (d0,d1,d2,d3,d4):
 *      00010--00011--00001--00000--00100--00101--00111--00110
 *      -15.5 -14.5 -13.5 -12.5 -11.5 -10.5 -9.5 -8.5
 *
 *      01010--01011--01001--01000--01100--01101--01111--01110
 *      -0.5 -1.5 -2.5 -3.5 -4.5 -5.5 -6.5 -7.5
 *
 *      11010--11011--11001--11000--11100--11101--11111--11110
 *      0.5 1.5 2.5 3.5 4.5 5.5 6.5 7.5
 *
 *      10010--10011--10001--10000--10100--10101--10111--10110
 *      15.5 14.5 13.5 12.5 11.5 10.5 9.5 8.5
 *
 * I dimension:
 * d0 is MSB and d3 is LSB in 16AM: (d0,d1,d2,d3):
 *
 *      0010---0011---0001---0000---0100---0101---0111---0110
 *      -7.5 -6.5 -5.5 -4.5 -3.5 -2.5 -1.5 -0.5
 *
 *      1010---1011---1001---1000---1100---1101---1111---1110
 *      7.5 6.5 5.5 4.5 3.5 2.5 1.5 0.5
 */

/*
 * deinterleave data:
 */
for(i = 0; i < INT_SIZE; i++)
    data_d[i] = data[i];
r_deileava(data_d, rule);

for(i = 0; i < INT_SIZE; i++)
{
    /* symbol 1, Q dimension: 32AM */
    d0 = data_d[i];
    d1 = data_d[i+1];
    d2 = Enc1[i];
    d3 = Enc2[i];
    d4 = Enc1[i+1];
    tx = 2*d2 - 2*d3 + 4*d2*d3 - 1.0 + (((2*d2-1)*(2*d3-1))<0?(d4-0.5):(0.5-d4));
    tx = (d1 == 0 ? (tx - 4) : (4 - tx));
    tx = (d0 == 0 ? (tx - 8) : (8 - tx));
    rx = tx + SIGMA_32AM_of_39_512QAM * gasdev();
    n = (-1.0) / (2 * SIGMA_32AM_of_39_512QAM * SIGMA_32AM_of_39_512QAM);
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
        exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
        exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
        exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
        exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
        exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)) +
        exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
        exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)))/
        (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
        exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
        exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
        exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
        exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +

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```

exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5)));

L_d1 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)))/
(exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)) +
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5))));

L_d2 = log((exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5))));

L_d3 = log((exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)))/
(exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-10.5)*(rx-10.5))));

L_d4 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-13.5)*(rx-13.5)))/
(exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+8.5)*(rx+8.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+15.5)*(rx+15.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-7.5)*(rx-7.5))+exp(n*(rx-8.5)*(rx-8.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-11.5)*(rx-11.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-15.5)*(rx-15.5))));

```


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```

D1_data[i]      = L_d0;
D1_data[i+1]    = L_d1;
  D1_parity[i]   = L_d2;
  D2_parity[i]   = L_d3;
  D1_parity[i+1] = L_d4;

  /* symbol 1, I dimension: 16AM */
d0 = data_d[i+2];
d1 = Encl[i+2];
d2 = Enc2[i+2];
d3 = Enc2[i+1];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4) : (4 - tx));
rx = tx + SIGMA_16AM_of_39_512QAM * gasdev();
n = (-1.0) / (2 * SIGMA_16AM_of_39_512QAM * SIGMA_16AM_of_39_512QAM);
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
  exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
  exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
  exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
  (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
  exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
  exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
  exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
  exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
  exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
  exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
  (exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
  exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
  exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
  exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
  exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
  exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
  exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
  (exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
  exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
  exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
  exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5))));

L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
  exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+2.5)*(rx+2.5)) +
  exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
  exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
  (exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+4.5)*(rx+4.5)) +
  exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
  exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5)) +
  exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-7.5)*(rx-7.5))));

D1_data[i+2]    = L_d0;
D1_parity[i+2]  = L_d1;
  D2_parity[i+2] = L_d2;
  D2_parity[i+1] = L_d3;
  i = i+2;
}
/*
* interleave data:
*/
r_ileav(D1_data, rule);

#endif

/*mio*/
#ifdef R12_16QAM
/*
* Channel: we transmit two 4-AM symbols to emulate a 16-QAM symbol.

```

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```

* 2 info bits and 2 parity bits are mapped to 1 16-QAM symbols which in
* turn are simulated as 2 4-AM symbols to achieve 2bit/s/Hz
* d0 is MSB and d1 is LSB in a 4-AM:(d0,d1) = 01--00-|-10--11
*                                     -3  -1   1   3
* INT_SIZE to be a multiple of 2
*/

n = (-1.0) / (2 * SIGMA_12_16QAM * SIGMA_12_16QAM);
for(i = 0; i < INT_SIZE; i++)
{
    /* symbol 1 */
    d0 = data[i];
    d1 = Enc1[i];
    tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
    rx = tx + SIGMA_12_16QAM * gasdev();
    L_d0 = log((exp(n*(rx-1)*(rx-1))+exp(n*(rx-3)*(rx-3))) /
               (exp(n*(rx+1)*(rx+1))+exp(n*(rx+3)*(rx+3))));
    L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3))) /
               (exp(n*(rx-1)*(rx-1))+exp(n*(rx+1)*(rx+1))));
    D1_data[i] = L_d0;
    D1_parity[i] = L_d1;
    D2_parity[i] = 0.0;

    /* symbol 2 */
    d0 = data[i+1];
    d1 = Enc2[i+1];
    tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
    rx = tx + SIGMA_12_16QAM * gasdev();
    L_d0 = log((exp(n*(rx-1)*(rx-1))+exp(n*(rx-3)*(rx-3))) /
               (exp(n*(rx+1)*(rx+1))+exp(n*(rx+3)*(rx+3))));
    L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3))) /
               (exp(n*(rx-1)*(rx-1))+exp(n*(rx+1)*(rx+1))));
    D1_data[i+1] = L_d0;
    D2_parity[i+1] = L_d1;
    D1_parity[i+1] = 0.0;

    i = i+1;
}
#endif

#ifdef R34_16QAM
/*
* Channel: we transmit two 4-AM symbols to emulate a 16-QAM symbol.
* 6 info bits and 2 parity bits are mapped to 2 16-QAM symbols which in
* turn are simulated as 4 4-AM symbols to achieve 3bit/s/Hz
* d0 is MSB and d1 is LSB in a 4-AM:(d0,d1) = 01--00-|-10--11
*                                     -3  -1   1   3
* INT_SIZE to be a multiple of 6
*/

n = (-1.0) / (2 * SIGMA_34_16QAM * SIGMA_34_16QAM);
for(i = 0; i < INT_SIZE; i++)
{
    /* symbol 1 */
    d0 = data[i];
    d1 = data[i+1];
    tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
    rx = tx + SIGMA_34_16QAM * gasdev();
    L_d0 = log((exp(n*(rx-1)*(rx-1))+exp(n*(rx-3)*(rx-3))) /
               (exp(n*(rx+1)*(rx+1))+exp(n*(rx+3)*(rx+3))));
    L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3))) /
               (exp(n*(rx-1)*(rx-1))+exp(n*(rx+1)*(rx+1))));
    D1_data[i] = L_d0;
    D1_data[i+1] = L_d1;

    /* symbol 2 */
    d0 = data[i+2];
    d1 = Enc1[i+1];
    tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
    rx = tx + SIGMA_34_16QAM * gasdev();
    L_d0 = log((exp(n*(rx-1)*(rx-1))+exp(n*(rx-3)*(rx-3))) /

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```

        (exp(n*(rx+1)*(rx+1))+exp(n*(rx+3)*(rx+3))));
L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3))) /
        (exp(n*(rx-1)*(rx-1))+exp(n*(rx+1)*(rx+1))));
D1_data[i+2] = L_d0;
D1_parity[i+1] = L_d1;

/* symbol 3 */
d0 = data[i+3];
d1 = data[i+4];
tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
rx = tx + SIGMA_34_16QAM * gasdev();
L_d0 = log((exp(n*(rx-1)*(rx-1))+exp(n*(rx-3)*(rx-3))) /
        (exp(n*(rx+1)*(rx+1))+exp(n*(rx+3)*(rx+3))));
L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3))) /
        (exp(n*(rx-1)*(rx-1))+exp(n*(rx+1)*(rx+1))));
D1_data[i+3] = L_d0;
D1_data[i+4] = L_d1;

/* symbol 4 */
d0 = data[i+5];
d1 = Enc2[i+4];
tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0;
rx = tx + SIGMA_34_16QAM * gasdev();
L_d0 = log((exp(n*(rx-1)*(rx-1))+exp(n*(rx-3)*(rx-3))) /
        (exp(n*(rx+1)*(rx+1))+exp(n*(rx+3)*(rx+3))));
L_d1 = log((exp(n*(rx+3)*(rx+3))+exp(n*(rx-3)*(rx-3))) /
        (exp(n*(rx-1)*(rx-1))+exp(n*(rx+1)*(rx+1))));
D1_data[i+5] = L_d0;
D2_parity[i+4] = L_d1;
D1_parity[i] = 0.0;
D1_parity[i+2] = 0.0;
D1_parity[i+3] = 0.0;
D1_parity[i+4] = 0.0;
D1_parity[i+5] = 0.0;
D2_parity[i] = 0.0;
D2_parity[i+1] = 0.0;
D2_parity[i+2] = 0.0;
D2_parity[i+3] = 0.0;
D2_parity[i+5] = 0.0;
i = i+5;
}
#endif

#ifdef R56_64QAM
/*
 * Channel:
 * d0 is MSB and d2 is LSB in 8AM: (d0,d1,d2):
 *      010---011---001---000---100---101---111---110
 *      -3.5  -2.5  -1.5  -0.5   0.5   1.5   2.5   3.5
 */
/*
 * Channel: we transmit two 8AM symbols to emulate a 64QAM symbol.
 * 10 info bits and 2 parity bits are mapped to 2 64QAM symbols which in
 * turn are simulated as 4 8AM symbols to achieve 5bit/s/Hz.
 *
 * INT_SIZE to be a multiple of 10
 */
n = (-1.0) / (2 * SIGMA_56_64QAM * SIGMA_56_64QAM);
for(i = 0; i < INT_SIZE; i++)
{
    /* symbol 1 */
    d0 = data[i];
    d1 = data[i+1];
    d2 = Enc1[i];
    tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
    rx = tx + SIGMA_56_64QAM * gasdev();
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
        exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
        (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
        exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

```

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L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
(exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));

D1_data[i] = L_d0;
D1_data[i+1] = L_d1;
D1_parity[i] = L_d2;
D1_parity[i+1] = 0;
D2_parity[i] = 0;
D2_parity[i+1] = 0;

/* symbol 2 */
d0 = data[i+2];
d1 = data[i+3];
d2 = data[i+4];
tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
rx = tx + SIGMA_56_64QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
(exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));

D1_data[i+2] = L_d0;
D1_data[i+3] = L_d1;
D1_data[i+4] = L_d2;
D1_parity[i+2] = 0;
D1_parity[i+3] = 0;
D1_parity[i+4] = 0;
D2_parity[i+2] = 0;
D2_parity[i+3] = 0;
D2_parity[i+4] = 0;

/* symbol 3 */
d0 = data[i+5];
d1 = data[i+6];
d2 = Enc2[i+5];
tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
rx = tx + SIGMA_56_64QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
(exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));

D1_data[i+5] = L_d0;
D1_data[i+6] = L_d1;
D2_parity[i+5] = L_d2;
D2_parity[i+6] = 0;
D1_parity[i+5] = 0;

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D1_parity[i+6] = 0;

/* symbol 4 */
d0 = data[i+7];
d1 = data[i+8];
d2 = data[i+9];
tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
rx = tx + SIGMA_56_64QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
            exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
            (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
            exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
            exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
            (exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
            exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
            exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
            (exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
            exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));
D1_data[i+7] = L_d0;
D1_data[i+8] = L_d1;
D1_data[i+9] = L_d2;
D1_parity[i+7] = 0;
D1_parity[i+8] = 0;
D1_parity[i+9] = 0;
D2_parity[i+7] = 0;
D2_parity[i+8] = 0;
D2_parity[i+9] = 0;

i = i+9;
}
#endif

#ifdef R57_128QAM
/*
 * Q dimension:
 * d0 is MSB and d2 is LSB in 8-AM: (d0,d1,d2):
 *      010---011---001---000---100---101---111---110
 *      -3.5  -2.5  -1.5  -0.5   0.5   1.5   2.5   3.5
 * I dimension:
 * d0 is MSB and d3 is LSB in 16AM: (d0,d1,d2,d3):
 *      0010---0011---0001---0000---0100---0101---0111---0110
 *      -7.5  -6.5  -5.5  -4.5  -3.5  -2.5  -1.5  -0.5
 *      1010---1011---1001---1000---1100---1101---1111---1110
 *      7.5   6.5   5.5   4.5   3.5   2.5   1.5   0.5
 *
 * INT_SIZE to be a multiple of 5
 */
for(i = 0; i < INT_SIZE; i++)
{
    /* Q dimension: 8AM */
    d0 = data[i];
    d1 = data[i+1];
    d2 = Encl[i];
    tx = 2*d0 - 2*d1 + 4*d0*d1 - 1.0 + (((2*d0-1)*(2*d1-1))<0?(d2-0.5):(0.5-d2));
    rx = tx + SIGMA_8AM_of_128QAM * gasdev();
    n = (-1.0) / (2 * SIGMA_8AM_of_128QAM * SIGMA_8AM_of_128QAM);
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
                exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5))));

    L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
                exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
                (exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
                exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));
}

```

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(exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5))));

L_d2 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx-1.5)*(rx-1.5))+exp(n*(rx-2.5)*(rx-2.5)))/
(exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5))));

D1_data[i] = L_d0;
D1_data[i+1] = L_d1;
D1_parity[i] = L_d2;
D1_parity[i+1] = 0.0;
D1_parity[i+2] = 0.0;
D1_parity[i+3] = 0.0;
D1_parity[i+4] = 0.0;

/* I dimension: 16AM */
d0 = data[i+2];
d1 = data[i+3];
d2 = data[i+4];
d3 = Enc2[i];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4) : (4 - tx));
rx = tx + SIGMA_16AM_of_128QAM * gasdev();
n = (-1.0) / (2 * SIGMA_16AM_of_128QAM * SIGMA_16AM_of_128QAM);
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5))));

L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
(exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-7.5)*(rx-7.5))));

D1_data[i+2] = L_d0;
D1_data[i+3] = L_d1;
D1_data[i+4] = L_d2;
D2_parity[i] = L_d3;
D2_parity[i+1] = 0.0;
D2_parity[i+2] = 0.0;
D2_parity[i+3] = 0.0;
D2_parity[i+4] = 0.0;

i = i+4;
}

```

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```

#endif

#ifdef R58_256QAM
/*
 * Channel:
 * d0 is MSB and d3 is LSB in 16AM: (d0,d1,d2,d3):
 *
 *      0010---0011---0001---0000---0100---0101---0111---0110
 *      -7.5   -6.5   -5.5   -4.5   -3.5   -2.5   -1.5   -0.5
 *
 *      1010---1011---1001---1000---1100---1101---1111---1110
 *      7.5    6.5    5.5    4.5    3.5    2.5    1.5    0.5
 *
 * Channel: we transmit two 16AM symbols to emulate a 256QAM symbol.
 * 10 info bits and 6 parity bits are mapped to 2 256QAM symbols which in
 * turn are simulated as 4 16AM symbols to achieve 6bit/s/Hz.
 *
 * INT_SIZE to be a multiple of 10
 */

n = (-1.0) / (2 * SIGMA_58_256QAM * SIGMA_58_256QAM);

/*
 * deinterleave data:
 */
for(i = 0; i < INT_SIZE; i++)
    data_d[i] = data[i];
r_deileava(data_d, rule);

for(i = 0; i < INT_SIZE; i++)
{
    /* symbol 1 */
    d0 = data_d[i];
    d1 = data_d[i+1];
    d2 = data_d[i+2];
    d3 = Encl[i];
    tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
    tx = (d0 == 0 ? (tx - 4) : (4 - tx));
    /* Test the mapping to the 16AM constellation:
     * if (i < 500)
     * printf("\n(%d%d%d%d) = %f", (int)d0, (int)d1, (int)d2, (int)d3, tx);
     */
    rx = tx + SIGMA_58_256QAM * gasdev();
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
        exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
        exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
        exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
        (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
        exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
        exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
        exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

    L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
        exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
        exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
        exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
        (exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
        exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
        exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
        exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

    L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
        exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
        exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
        exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
        (exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
        exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
        exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
        exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5))));
}

```

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L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
(exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-7.5)*(rx-7.5))));

D1_data[i]      = L_d0;
D1_data[i+1]    = L_d1;
D1_data[i+2]    = L_d2;
D1_parity[i]    = L_d3;
D1_parity[i+1] = 0;
D1_parity[i+2] = 0;
D2_parity[i]    = 0;
D2_parity[i+1] = 0;

/* symbol 2 */
d0 = data_d[i+3];
d1 = data_d[i+4];
d2 = Enc2[i+2];
d3 = Enc1[i+4];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4) : (4 - tx));
rx = tx + SIGMA_58_256QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5))));

L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
(exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-7.5)*(rx-7.5))));

D1_data[i+3]    = L_d0;
D1_data[i+4]    = L_d1;
D2_parity[i+2] = L_d2;
D1_parity[i+4] = L_d3;
D1_parity[i+3] = 0;
D2_parity[i+3] = 0;
D2_parity[i+4] = 0;

/* symbol 3 */
d0 = data_d[i+5];

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d1 = data_d[i+6];
d2 = data_d[i+7];
d3 = Enc2[i+5];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4): (4 - tx));
rx = tx + SIGMA_58_256QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5))));

L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
(exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-7.5)*(rx-7.5))));

D1_data[i+5] = L_d0;
D1_data[i+6] = L_d1;
D1_data[i+7] = L_d2;
D2_parity[i+5] = L_d3;
D2_parity[i+6] = 0;
D2_parity[i+7] = 0;
D1_parity[i+5] = 0;
D1_parity[i+6] = 0;

/* symbol 4 */
d0 = data_d[i+8];
d1 = data_d[i+9];
d2 = Enc1[i+7];
d3 = Enc2[i+9];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4): (4 - tx));
rx = tx + SIGMA_58_256QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/

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(exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)));

L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5))));

L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
(exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-7.5)*(rx-7.5))));

D1_data[i+8] = L_d0;
D1_data[i+9] = L_d1;
D1_parity[i+7] = L_d2;
D2_parity[i+9] = L_d3;
D1_parity[i+8] = 0;
D1_parity[i+9] = 0;
D2_parity[i+7] = 0;
D2_parity[i+8] = 0;

i = i+9;
}
/*
* interleave data:
*/
r_ileav(D1_data, rule);
#endif

#ifdef R68_256QAM
/*
* Channel:
* d0 is MSB and d3 is LSB in 16AM: (d0,d1,d2,d3):
*
*      0010---0011---0001---0000---0100---0101---0111---0110
*      -7.5   -6.5   -5.5   -4.5   -3.5   -2.5   -1.5   -0.5
*
*      1010---1011---1001---1000---1100---1101---1111---1110
*      7.5     6.5     5.5     4.5     3.5     2.5     1.5     0.5
*
* Channel: we transmit two 16AM symbols to emulate a 256QAM symbol.
* 6 info bits and 2 parity bits are mapped to one 256QAM symbol which in
* turn is simulated as 2 16AM symbols to achieve 6bit/s/Hz.
*
* INT_SIZE to be a multiple of 6
*/
n = (-1.0) / (2 * SIGMA_68_256QAM * SIGMA_68_256QAM);

/*
* deinterleave data:
*/
for(i = 0; i < INT_SIZE; i++)
    data_d[i] = data[i];
r_deileava(data_d, rule);

for(i = 0; i < INT_SIZE; i++)
{
    /* symbol 1 */
    d0 = data_d[i];
    d1 = data_d[i+1];

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d2 = data_d[i+2];
d3 = Enc1[i];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4): (4 - tx));
rx = tx + SIGMA_68_256QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5))));

L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
(exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-7.5)*(rx-7.5))));

D1_data[i] = L_d0;
D1_data[i+1] = L_d1;
D1_data[i+2] = L_d2;
D1_parity[i] = L_d3;
D1_parity[i+1] = 0;
D1_parity[i+2] = 0;
D2_parity[i] = 0;
D2_parity[i+1] = 0;
D2_parity[i+2] = 0;

/* symbol 2 */
d0 = data_d[i+3];
d1 = data_d[i+4];
d2 = data_d[i+5];
d3 = Enc2[i+3];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4): (4 - tx));
rx = tx + SIGMA_68_256QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +

```

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exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)));

L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)));

L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
(exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-7.5)*(rx-7.5)));

D1_data[i+3] = L_d0;
D1_data[i+4] = L_d1;
D1_data[i+5] = L_d2;
D2_parity[i+3] = L_d3;
D2_parity[i+4] = 0;
D2_parity[i+5] = 0;
D1_parity[i+3] = 0;
D1_parity[i+4] = 0;
D1_parity[i+5] = 0;

i = i+5;
)

/*
* interleave data:
*/
r_ileav(D1_data, rule);

#endif

#ifdef R69_512QAM
/*
* Interleaver should be a multiple of 12, e.g., 6144
*
* Q dimension:
* d0 is MSB and d4 is LSB in 32AM: (d0,d1,d2,d3,d4):
* 00010--00011--00001--00000--00100--00101--00111--00110
* -15.5 -14.5 -13.5 -12.5 -11.5 -10.5 -9.5 -8.5
*
* 01010--01011--01001--01000--01100--01101--01111--01110
* -0.5 -1.5 -2.5 -3.5 -4.5 -5.5 -6.5 -7.5
*
* 11010--11011--11001--11000--11100--11101--11111--11110
* 0.5 1.5 2.5 3.5 4.5 5.5 6.5 7.5
*
* 10010--10011--10001--10000--10100--10101--10111--10110
* 15.5 14.5 13.5 12.5 11.5 10.5 9.5 8.5
*
* I dimension:
* d0 is MSB and d3 is LSB in 16AM: (d0,d1,d2,d3):
*
* 0010---0011---0001---0000---0100---0101---0111---0110
* -7.5 -6.5 -5.5 -4.5 -3.5 -2.5 -1.5 -0.5
*
* 1010---1011---1001---1000---1100---1101---1111---1110
* 7.5 6.5 5.5 4.5 3.5 2.5 1.5 0.5

```

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```

*/
/*
* deinterleave data:
*/
for(i = 0; i < INT_SIZE; i++)
    data_d[i] = data[i];
r_deileava(data_d, rule);

for(i = 0; i < INT_SIZE; i++)
{
    /* symbol 1, Q dimension: 32AM */
    d0 = data_d[i];
    d1 = data_d[i+1];
    d2 = data_d[i+2];
    d3 = data_d[i+3];
    d4 = Encl[i];
    tx = 2*d2 - 2*d3 + 4*d2*d3 - 1.0 + (((2*d2-1)*(2*d3-1))<0?(d4-0.5):(0.5-d4));
    tx = (d1 == 0 ? (tx - 4) : (4 - tx));
    tx = (d0 == 0 ? (tx - 8) : (8 - tx));
    rx = tx + SIGMA_32AM_of_512QAM * gasdev();
    n = (-1.0) / (2 * SIGMA_32AM_of_512QAM * SIGMA_32AM_of_512QAM);
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
        exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
        exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
        exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
        exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
        exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)) +
        exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
        exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)))/
        (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
        exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
        exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
        exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
        exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
        exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
        exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
        exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5))));

    L_d1 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
        exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
        exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
        exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
        exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
        exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
        exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
        exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)))/
        (exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
        exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)) +
        exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
        exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)) +
        exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
        exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
        exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
        exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5))));

    L_d2 = log((exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
        exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
        exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
        exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
        exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
        exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
        exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
        exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)))/
        (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
        exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
        exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
        exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5)) +
        exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
        exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
        exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +

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exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5))));

L_d3 = log((exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)))/
(exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-10.5)*(rx-10.5))));

L_d4 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-13.5)*(rx-13.5)))/
(exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+8.5)*(rx+8.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+15.5)*(rx+15.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-7.5)*(rx-7.5))+exp(n*(rx-8.5)*(rx-8.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-11.5)*(rx-11.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-15.5)*(rx-15.5))));

D1_data[i]      = L_d0;
D1_data[i+1]    = L_d1;
D1_data[i+2]    = L_d2;
D1_data[i+3]    = L_d3;
D1_parity[i]    = L_d4;
D1_parity[i+1]  = 0.0;
D1_parity[i+2]  = 0.0;
D1_parity[i+3]  = 0.0;
D1_parity[i+5]  = 0.0;

/* symbol 1, I dimension: 16AM */
d0 = data_d[i+4];
d1 = data_d[i+5];
d2 = Enc1[i+4];
d3 = Enc2[i+2];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4) : (4 - tx));
rx = tx + SIGMA_16AM_of_512QAM * gasdev();
n = (-1.0) / (2 * SIGMA_16AM_of_512QAM * SIGMA_16AM_of_512QAM);
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +

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exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)));

L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5))));

L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
(exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-7.5)*(rx-7.5))));

D1_data[i+4] = L_d0;
D1_data[i+5] = L_d1;
D1_parity[i+4] = L_d2;
D2_parity[i+2] = L_d3;
D2_parity[i] = 0.0;
D2_parity[i+1] = 0.0;
D2_parity[i+3] = 0.0;
D2_parity[i+4] = 0.0;
D2_parity[i+5] = 0.0;

/* symbol 2, Q dimension: 32AM */
d0 = data_d[i+6];
d1 = data_d[i+7];
d2 = data_d[i+8];
d3 = data_d[i+9];
d4 = Enc2[i+6];
tx = 2*d2 - 2*d3 + 4*d2*d3 - 1.0 + (((2*d2-1)*(2*d3-1))<0?(d4-0.5):(0.5-d4));
tx = (d1 == 0 ? (tx - 4) : (4 - tx));
tx = (d0 == 0 ? (tx - 8) : (8 - tx));
rx = tx + SIGMA_32AM_of_512QAM * gasdev();
n = (-1.0) / (2 * SIGMA_32AM_of_512QAM * SIGMA_32AM_of_512QAM);
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5))));

L_d1 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)))/
(exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)) +

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exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5)));

L_d2 = log((exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5))));

L_d3 = log((exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)))/
(exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-10.5)*(rx-10.5))));

L_d4 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-13.5)*(rx-13.5)))/
(exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+8.5)*(rx+8.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+15.5)*(rx+15.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-7.5)*(rx-7.5))+exp(n*(rx-8.5)*(rx-8.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-11.5)*(rx-11.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-15.5)*(rx-15.5))));

D1_data[i+6] = L_d0;
D1_data[i+7] = L_d1;
D1_data[i+8] = L_d2;
D1_data[i+9] = L_d3;
D2_parity[i+6] = L_d4;
D2_parity[i+7] = 0.0;
D2_parity[i+8] = 0.0;
D2_parity[i+9] = 0.0;
D2_parity[i+11] = 0.0;

/* symbol 2, I dimension: 16AM */
d0 = data_d[i+10];
d1 = data_d[i+11];
d2 = Enc2[i+10];

```


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d3 = Encl[i+8];
tx = 2*d1 - 2*d2 + 4*d1*d2 - 1.0 + (((2*d1-1)*(2*d2-1))<0?(d3-0.5):(0.5-d3));
tx = (d0 == 0 ? (tx - 4) : (4 - tx));
rx = tx + SIGMA_16AM_of_512QAM * gasdev();
n = (-1.0) / (2 * SIGMA_16AM_of_512QAM * SIGMA_16AM_of_512QAM);
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d1 = log((exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)))/
(exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5))));

L_d2 = log((exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)))/
(exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5))));

L_d3 = log((exp(n*(rx+5.5)*(rx+5.5))+exp(n*(rx+6.5)*(rx+6.5)) +
exp(n*(rx+1.5)*(rx+1.5))+exp(n*(rx+2.5)*(rx+2.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)))/
(exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+4.5)*(rx+4.5)) +
exp(n*(rx+3.5)*(rx+3.5))+exp(n*(rx+0.5)*(rx+0.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-7.5)*(rx-7.5))));

D1_data[i+10] = L_d0;
D1_data[i+11] = L_d1;
D2_parity[i+10] = L_d2;
D1_parity[i+8] = L_d3;
D1_parity[i+6] = 0.0;
D1_parity[i+7] = 0.0;
D1_parity[i+9] = 0.0;
D1_parity[i+10] = 0.0;
D1_parity[i+11] = 0.0;

i = i+11;
}
/*
* interleave data:
*/
r_ileav(D1_data, rule);

#endif

#ifdef R710_1024QAM
/*
* Use S2044_33_1 interleaver (multiple of 14)
*
* I and Q dimensions:
* d0 is MSB and d4 is LSB in 32AM: (d0,d1,d2,d3,d4):
* 00010--00011--00001--00000--00100--00101--00111--00110
* -15.5 -14.5 -13.5 -12.5 -11.5 -10.5 -9.5 -8.5
*
* 01010--01011--01001--01000--01100--01101--01111--01110

```

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*      -0.5   -1.5   -2.5   -3.5   -4.5   -5.5   -6.5   -7.5
*
*      11010--11011--11001--11000--11100--11101--11111--11110
*      0.5    1.5    2.5    3.5    4.5    5.5    6.5    7.5
*
*      10010--10011--10001--10000--10100--10101--10111--10110
*      15.5   14.5   13.5   12.5   11.5   10.5   9.5    8.5
*
*/

n = (-1.0) / (2 * SIGMA_710_1024QAM * SIGMA_710_1024QAM);
for(i = 0; i < INT_SIZE; i++)
{
    /* symbol 1, Q dimension */
    d0 = data[i];
    d1 = data[i+1];
    d2 = data[i+2];
    d3 = data[i+3];
    d4 = Encl[i];
    tx = 2*d2 - 2*d3 + 4*d2*d3 - 1.0 + (((2*d2-1)*(2*d3-1))<0?(d4-0.5):(0.5-d4));
    tx = (d1 == 0 ? (tx - 4) : (4 - tx));
    tx = (d0 == 0 ? (tx - 8) : (8 - tx));
    rx = tx + SIGMA_710_1024QAM * gasdev();
    L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
        exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
        exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
        exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
        exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
        exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)) +
        exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
        exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)))/
        (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
        exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
        exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
        exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
        exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
        exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
        exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
        exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5))));

    L_d1 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
        exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
        exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
        exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
        exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
        exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
        exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
        exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)))/
        (exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
        exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)) +
        exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
        exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)) +
        exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
        exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
        exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
        exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5))));

    L_d2 = log((exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
        exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
        exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
        exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
        exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
        exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
        exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
        exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)))/
        (exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
        exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
        exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
        exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5)) +
        exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
        exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +

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exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)));

L_d3 = log((exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)))/
(exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-10.5)*(rx-10.5))));

L_d4 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-13.5)*(rx-13.5)))/
(exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+8.5)*(rx+8.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+15.5)*(rx+15.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-7.5)*(rx-7.5))+exp(n*(rx-8.5)*(rx-8.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-11.5)*(rx-11.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-15.5)*(rx-15.5))));

Dl_data[i]      = L_d0;
Dl_data[i+1]    = L_d1;
Dl_data[i+2]    = L_d2;
Dl_data[i+3]    = L_d3;
Dl_data[i+4]    = L_d4;
Dl_parity[i]    = L_d4;
Dl_parity[i+1]  = 0.0;
Dl_parity[i+2]  = 0.0;
Dl_parity[i+3]  = 0.0;
Dl_parity[i+4]  = 0.0;
Dl_parity[i+6]  = 0.0;

/* symbol 1, I dimension */
d0 = data[i+4];
d1 = data[i+5];
d2 = data[i+6];
d3 = Enc1[i+5];
d4 = Enc2[i];
tx = 2*d2 - 2*d3 + 4*d2*d3 - 1.0 + (((2*d2-1)*(2*d3-1))<0?(d4-0.5):(0.5-d4));
tx = (d1 == 0 ? (tx - 4): (4 - tx));
tx = (d0 == 0 ? (tx - 8): (8 - tx));
rx = tx + SIGMA_710_1024QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +

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```
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5))));
```

```
L_d1 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)))/
(exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)) +
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5))));
```

```
L_d2 = log((exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5))));
```

```
L_d3 = log((exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)))/
(exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-10.5)*(rx-10.5))));
```

```
L_d4 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-13.5)*(rx-13.5)))/
(exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+8.5)*(rx+8.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+15.5)*(rx+15.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-7.5)*(rx-7.5))+exp(n*(rx-8.5)*(rx-8.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-11.5)*(rx-11.5)) +
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exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-15.5)*(rx-15.5)));

D1_data[i+4] = L_d0;
D1_data[i+5] = L_d1;
D1_data[i+6] = L_d2;
D1_parity[i+5] = L_d3;
D2_parity[i] = L_d4;
D2_parity[i+1] = 0.0;
D2_parity[i+2] = 0.0;
D2_parity[i+3] = 0.0;
D2_parity[i+4] = 0.0;
D2_parity[i+6] = 0.0;

/* symbol 2, Q dimension */
d0 = data[i+7];
d1 = data[i+8];
d2 = data[i+9];
d3 = data[i+10];
d4 = Enc2[i+5];
tx = 2*d2 - 2*d3 + 4*d2*d3 - 1.0 + (((2*d2-1)*(2*d3-1))<0?(d4-0.5):(0.5-d4));
tx = (d1 == 0 ? (tx - 4) : (4 - tx));
tx = (d0 == 0 ? (tx - 8) : (8 - tx));
rx = tx + SIGMA_710_1024QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5))));

L_d1 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)))/
(exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)) +
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5))));

L_d2 = log((exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +

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exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)));

L_d3 = log((exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)))/
(exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-10.5)*(rx-10.5))));

L_d4 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-13.5)*(rx-13.5)))/
(exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+8.5)*(rx+8.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+15.5)*(rx+15.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-7.5)*(rx-7.5))+exp(n*(rx-8.5)*(rx-8.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-11.5)*(rx-11.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-15.5)*(rx-15.5))));

D1_data[i+7] = L_d0;
D1_data[i+8] = L_d1;
D1_data[i+9] = L_d2;
D1_data[i+10] = L_d3;
D2_parity[i+5] = L_d4;
D2_parity[i+7] = 0.0;
D2_parity[i+8] = 0.0;
D2_parity[i+9] = 0.0;
D2_parity[i+11] = 0.0;
D2_parity[i+12] = 0.0;
D2_parity[i+13] = 0.0;

/* symbol 2, I dimension */
d0 = data[i+11];
d1 = data[i+12];
d2 = data[i+13];
d3 = Enc2[i+10];
d4 = Enc1[i+10];
tx = 2*d2 - 2*d3 + 4*d2*d3 - 1.0 + (((2*d2-1)*(2*d3-1))<0?(d4-0.5):(0.5-d4));
tx = (d1 == 0 ? (tx - 4) : (4 - tx));
tx = (d0 == 0 ? (tx - 8) : (8 - tx));
rx = tx + SIGMA_710_1024QAM * gasdev();
L_d0 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +

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exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5)));

L_d1 = log((exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)))/
(exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)) +
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5))));

L_d2 = log((exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-11.5)*(rx-11.5)))/
(exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5))));

L_d3 = log((exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+7.5)*(rx+7.5)) +
exp(n*(rx+8.5)*(rx+8.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+15.5)*(rx+15.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-7.5)*(rx-7.5)) +
exp(n*(rx-8.5)*(rx-8.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-15.5)*(rx-15.5)))/
(exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-13.5)*(rx-13.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-10.5)*(rx-10.5))));

L_d4 = log((exp(n*(rx+2.5)*(rx+2.5))+exp(n*(rx+1.5)*(rx+1.5)) +
exp(n*(rx+6.5)*(rx+6.5))+exp(n*(rx+5.5)*(rx+5.5)) +
exp(n*(rx+10.5)*(rx+10.5))+exp(n*(rx+9.5)*(rx+9.5)) +
exp(n*(rx+14.5)*(rx+14.5))+exp(n*(rx+13.5)*(rx+13.5)) +
exp(n*(rx-2.5)*(rx-2.5))+exp(n*(rx-1.5)*(rx-1.5)) +
exp(n*(rx-6.5)*(rx-6.5))+exp(n*(rx-5.5)*(rx-5.5)) +
exp(n*(rx-10.5)*(rx-10.5))+exp(n*(rx-9.5)*(rx-9.5)) +
exp(n*(rx-14.5)*(rx-14.5))+exp(n*(rx-13.5)*(rx-13.5)))/
(exp(n*(rx+4.5)*(rx+4.5))+exp(n*(rx+3.5)*(rx+3.5)) +
exp(n*(rx+7.5)*(rx+7.5))+exp(n*(rx+8.5)*(rx+8.5)) +
exp(n*(rx+12.5)*(rx+12.5))+exp(n*(rx+11.5)*(rx+11.5)) +
exp(n*(rx+0.5)*(rx+0.5))+exp(n*(rx+15.5)*(rx+15.5)) +
exp(n*(rx-4.5)*(rx-4.5))+exp(n*(rx-3.5)*(rx-3.5)) +
exp(n*(rx-7.5)*(rx-7.5))+exp(n*(rx-8.5)*(rx-8.5)) +

```

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```

exp(n*(rx-12.5)*(rx-12.5))+exp(n*(rx-11.5)*(rx-11.5)) +
exp(n*(rx-0.5)*(rx-0.5))+exp(n*(rx-15.5)*(rx-15.5)));

D1_data[i+11] = L_d0;
D1_data[i+12] = L_d1;
D1_data[i+13] = L_d2;
D2_parity[i+10] = L_d3;
D1_parity[i+10] = L_d4;
D1_parity[i+7] = 0.0;
D1_parity[i+8] = 0.0;
D1_parity[i+9] = 0.0;
D1_parity[i+11] = 0.0;
D1_parity[i+12] = 0.0;
D1_parity[i+13] = 0.0;

i = i+13;
}
#endif

/*****

/*
* At this moment we received the whole turbo code block:
* D1_data[] stores the received information sequence,
* D1_parity[] stores the received punctured parity P sequence and
* D2_data[] stores the interleaved received information sequence,
*/

for(i = 0; i < INT_SIZE; i++)
    D2_data[i] = D1_data[i];
r_ileav(D2_data, rule);
/*
* D2_parity[] stores the received punctured parity Q sequence.
*/

for(iteration = 1; iteration <= NR_ITER; iteration++)
{
    /*
    * Start one iteration of the turbo decoder here:
    */
#ifdef R46_64QAM_TTCM_VoCAL
    jat_map2(jat_codel, D1_data, D1_parity, D1_app, D1_exi);
#else
    jat_map1(jat_codel, D1_data, D1_parity, D1_app, D1_exi);
#endif
    /*
    * Interleave the extrinsic information from Decoder1:
    */
    for(k = 0; k < INT_SIZE; k++)
        D2_app[k] = D1_exi[k];
    r_ileav(D2_app, rule);

    /*
    * Decoder2:
    */
#ifdef R46_64QAM_TTCM_VoCAL
    jat_map2(jat_code2, D2_data, D2_parity, D2_app, D2_exi);
#else
    jat_map1(jat_code2, D2_data, D2_parity, D2_app, D2_exi);
#endif

    /*
    * Deinterleave the extrinsic information from Decoder2:
    */
    r_deileav(D2_exi, rule);
    for(k = 0; k < INT_SIZE; k++)
        D1_app[k] = D2_exi[k];
}

```


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```

#ifdef R46_64QAM_TTCM_VoCAL
for(k = 0; k < INT_SIZE/2; k++)
    Dec_data[k] = D1_data[k] + log(D1_exi[k]) + log(D2_exi[k]);

/*
 * Re-encode with encoder1:
 */
jat_code1->enc_state = 0;          /* reset encoder1's state */
for(k = 0; k < INT_SIZE/2; k++)
    Enc1[k] = jat_enc_bp_fp(jat_code1, ((Dec_data[k] > 0.0)?1:0));

/*
 * interleave data:
 */
for(k = 0; k < INT_SIZE/2; k++)
    data_i[k] = ((Dec_data[k] > 0.0)?1:0);
r_ileava(data_i, rule);

/*
 * Re-encode with encoder2:
 */
jat_code2->enc_state = 0;          /* reset encoder2's state */
for(k = 0; k < INT_SIZE/2; k++)
    Enc2[k] = jat_enc_bp_fp(jat_code2, data_i[k]);

/*
 * Find the closest point out of four in the sub-constellation
 */
for(k = 0; k < INT_SIZE/2 - 1; )
{
    u4 = ((Dec_data[k] > 0.0)?1:0);
    u3 = ((Dec_data[k+1] > 0.0)?1:0);
    u2 = Enc1[k];
    u1 = Enc2[k+1];

    rx_I = D1_data[k + INT_SIZE/2];
    rx_Q = D1_data[k + INT_SIZE/2 + 1];

    j = 4*u4+8*u3+16*u2+32*u1;
    v00_I = find_tx_I(j);
    v00_Q = find_tx_Q(j);
    v01_I = find_tx_I(j+1);
    v01_Q = find_tx_Q(j+1);
    v10_I = find_tx_I(j+2);
    v10_Q = find_tx_Q(j+2);
    v11_I = find_tx_I(j+3);
    v11_Q = find_tx_Q(j+3);

    Dec_data[k+INT_SIZE/2] = log(
        (exp(n*((rx_I-v11_I)*(rx_I-v11_I)+(rx_Q-v11_Q)*(rx_Q-v11_Q)))+
        exp(n*((rx_I-v10_I)*(rx_I-v10_I)+(rx_Q-v10_Q)*(rx_Q-v10_Q)))/
        (exp(n*((rx_I-v01_I)*(rx_I-v01_I)+(rx_Q-v01_Q)*(rx_Q-v01_Q)))+
        exp(n*((rx_I-v00_I)*(rx_I-v00_I)+(rx_Q-v00_Q)*(rx_Q-v00_Q)))));

    Dec_data[k+INT_SIZE/2+1] = log(
        (exp(n*((rx_I-v11_I)*(rx_I-v11_I)+(rx_Q-v11_Q)*(rx_Q-v11_Q)))+
        exp(n*((rx_I-v01_I)*(rx_I-v01_I)+(rx_Q-v01_Q)*(rx_Q-v01_Q)))/
        (exp(n*((rx_I-v10_I)*(rx_I-v10_I)+(rx_Q-v10_Q)*(rx_Q-v10_Q)))+
        exp(n*((rx_I-v00_I)*(rx_I-v00_I)+(rx_Q-v00_Q)*(rx_Q-v00_Q)))));

    k = k+2;
}

#else
for(k = 0; k < INT_SIZE; k++)
    Dec_data[k] = D1_data[k] + log(D1_exi[k]) + log(D2_exi[k]);
#endif

/*

```

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```

    * print errors:
    */
    k = print_err(data, Dec_data, iteration, block, no_err);
    if(k == 0)
        break;

    /*
    * End one iteration of the turbo decoder here.
    */
}

}

free(jat_code1->P0state);
free(jat_code1->P1state);
free(jat_code1->N0state);
free(jat_code1->N1state);
free(jat_code1->Coded0);
free(jat_code1->Coded1);
free(jat_code1);
free(jat_code2->P0state);
free(jat_code2->P1state);
free(jat_code2->N0state);
free(jat_code2->N1state);
free(jat_code2->Coded0);
free(jat_code2->Coded1);
free(jat_code2);
free(rule);
free(data);
free(data_i);
free(data_d);
free(no_err);
free(Enc1);
free(Enc2);
free(D1_data);
free(D1_parity);
free(D1_app);
free(D1_exi);
free(D2_data);
free(D2_parity);
free(D2_app);
free(D2_exi);
free(Dec_data);
free(frame_hist);
free(Zero_data);
for(i = THRESHOLD_ITER; i <= NR_ITER; i++)
    free(bit_hist_array[i]);
free(bit_hist_array);
free(bit_hist_block);
}

/*****
/* jat_trellis_bp_fp() initializes the code structure */
void jat_trellis_bp_fp(jat_code *code_str)
{
    int i;
    for(i = 0; i < code_str->nr_states ; i++)
    {
        code_str->enc_state = i;
        code_str->P0state[i] = jat_ps(code_str, 0);
        code_str->P1state[i] = jat_ps(code_str, 1);
        code_str->enc_state = i;
        code_str->Coded0[i] = jat_enc_bp_fp(code_str, 0);
        code_str->N0state[i] = code_str->enc_state; /*next state i if d = 0 */
        code_str->enc_state = i;
        code_str->Coded1[i] = jat_enc_bp_fp(code_str, 1);
        code_str->N1state[i] = code_str->enc_state; /*next state i if d = 1 */
    }
}

```

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```

/*****
/* jat_ps() returns the previous state, given the code structure & the input */
/*      bit for the previous state */
/*      input:  current state, input bit for the previous state */
/*      output: previous state */
int jat_ps(jat_code *code_st, int inp)
{
    int pr_state, pr_msb, i, j, k, l;

    if(code_st->enc_mem == 1)
    {
        pr_state = code_st->enc_state ^ inp;
    }
    else
    {
        /*find previous state: */
        pr_msb = (inp & 0x1) ^ (code_st->enc_state & 0x1);
        for(i=1,j=2,k=(1 << code_st->enc_mem-1),l=code_st->enc_mem-1;i<code_st->enc_mem;i++,l--)
        {
            pr_msb = pr_msb ^ (((code_st->enc_state&j)>>i) & ((code_st->bp&k)>>l));
            j = j << 1;
            k = k >> 1;
        }

        pr_state = ((code_st->enc_state >> 1) & ((1<<(code_st->enc_mem - 1)) - 1)) |
            (pr_msb << (code_st->enc_mem - 1));
    }
    return (pr_state);
}

/*****
/* jat_enc_bp_fp() - rate 1/2 systematic feedback convolutional enc. */
/*      input:  input bit to be encoded */
/*      output: the coded bit */
/* Note:      the lsb of the enc_state will have the new input bit */
/*      the msb of the enc_state matches the lsb of bp & fp */
int jat_enc_bp_fp(jat_code *code_st, int data)
{
    int new_lsb, parity, i, j, k, l;

    new_lsb = data;
    if(code_st->enc_mem == 1)
    {
        parity = code_st->enc_state ^ data;
        code_st->enc_state = parity;
    }
    else
    {
        /* xor it with the bits of the enc_state1 for which bpl is one */
        for(i = 0, j = 1, k = (1 << code_st->enc_mem-1), l = code_st->enc_mem - 1; i < code_st->enc_mem; i++, l--)
        {
            new_lsb = new_lsb ^ (((code_st->enc_state&j)>>i) & ((code_st->bp&k)>>l));
            j = j << 1;
            k = k >> 1;
        }

        /* find the parity bit */
        parity = new_lsb & ((code_st->fp&(1<<code_st->enc_mem)) >> code_st->enc_mem);
        for(i = 0, j = 1, k = (1 << code_st->enc_mem-1), l = code_st->enc_mem - 1; i < code_st->enc_mem; i++, l--)
        {
            parity = parity ^ (((code_st->enc_state&j)>>i) & ((code_st->fp&k)>>l));
            j = j << 1;
            k = k >> 1;
        }
    }
}

```

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```

        /* update code_st->enc_state */
        code_st->enc_state = ((code_st->enc_state & (code_st->nr_states/2 - 1)) << 1) |
new_lsb;
    }
    return (parity);
}

/*****
void r_ileav(double *array, int *rule_i)
{
    double *i_wmem;
    int k;

    i_wmem = (double *)malloc(sizeof(double) * INT_SIZE);
    if(i_wmem == 0)
        printf("\nCouldn't allocate i_wmem memory!");
    for(k = 0; k < INT_SIZE; k++)
        i_wmem[k] = array[k];
    for(k = 0; k < INT_SIZE; k++)
        array[k] = i_wmem[rule_i[2*k+1]];
    free(i_wmem);
}

/*****
void r_ileava(int *array, int *rule_i)
{
    int *i_wmem;
    int k;

    i_wmem = (int *)malloc(sizeof(int) * INT_SIZE);
    if(i_wmem == 0)
        printf("\nCouldn't allocate i_wmem memory!");
    for(k = 0; k < INT_SIZE; k++)
        i_wmem[k] = array[k];
    for(k = 0; k < INT_SIZE; k++)
        array[k] = i_wmem[rule_i[2*k+1]];
    free(i_wmem);
}

/*****
void r_deileav(double *array, int *rule_d)
{
    double *d_wmem;
    int k;

    d_wmem = (double *)malloc(sizeof(double) * INT_SIZE);
    if(d_wmem == 0)
        printf("\nCouldn't allocate d_wmem memory!");
    for(k = 0; k < INT_SIZE; k++)
        d_wmem[rule_d[2*k+1]] = array[k];
    for(k = 0; k < INT_SIZE; k++)
        array[k] = d_wmem[k];
    free(d_wmem);
}

/*****
void r_deileava(int *array, int *rule_d)
{
    int *d_wmem;
    int k;

    d_wmem = (int *)malloc(sizeof(int) * INT_SIZE);
    if(d_wmem == 0)
        printf("\nCouldn't allocate d_wmem memory!");
    for(k = 0; k < INT_SIZE; k++)
        d_wmem[rule_d[2*k+1]] = array[k];
    for(k = 0; k < INT_SIZE; k++)

```

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```

    array[k] = d_wmem[k];
    free(d_wmem);
}

/*****
/* nrgen() returns a random number between 0 and 1
/* (uniform distribution generator)
double nrgen()
{
    long z, k;

    k = s1 / 53668;
    s1 = 40014 * (s1 - k * 53668) - k * 12211;
    if(s1 < 0)
        s1 += 2147483563;
    k = s2 / 52774;
    s2 = 40692 * (s2 - k * 52774) - k * 3791;
    if(s2 < 0)
        s2 += 2147483399;
    z = s1 - s2;
    if(z < 1)
        z += 2147483562;
    return ((double)z / 2147483563);
}

/*****
/* nrgenbin() returns a 0 or 1 (uniform distribution)
int nrgenbin()
{
    return ((nrgen() > 0.5)?1:0);
}

/*****
/* gasdev() returns a normally distributed deviate
/* with zero mean and unit variance
double gasdev()
{
    static int      iset = 0;
    static double   gset;
    double          fac, r, v1, v2;

    if(iset == 0)
    {
        /* pick two uniform numbers in the square extending from
        /* -1 to +1 in each direction, see if they are in the
        /* unit circle, and if they are not, try again.
        do
        {
            v1 = 2.0 * nrgen() - 1.0;
            v2 = 2.0 * nrgen() - 1.0;
            r = v1 * v1 + v2 * v2;

            while (r >= 1.0 || r == 0.0);
            fac = sqrt(-2.0 * log(r)/r);
            /* now make the Box-Muller transformation to get two normal
            /* deviates; return one and save the other for next time.
            gset = v1 * fac;
            iset = 1;          /* set flag
            return (v2 * fac);
        }
    }
    else
    {
        /* we have an extra deviate handy, so unset the flag and
        /* return it.
        iset = 0;
        return (gset);
    }
}

```

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```

/*****
/* errors() returns the nr. of positions in which two blocks of data are */
/* different; it accepts a shift between the addresses */
/* inputs: the address of the first block of integers */
/*          the address of the second block of doubles */
/*          the size of the block (blocks are equal) */
/* output: the number of positions in which the two blocks are dif. */
int errors(int *block1, double *block2, int size, int iter_nr)
{
    int i;
    int count = 0;

    for(i = 0; i < size; i++)
        if(block1[i] != ((block2[i] > 0.0)?1:0))
        {
            count++;
#ifdef BIT_HIST
            if(iter_nr>=THRESHOLD_ITER)
            {
                *bit_hist_array[iter_nr] = bit_hist_block[iter_nr];
                bit_hist_array[iter_nr]++;
                *bit_hist_array[iter_nr] = i;
                bit_hist_array[iter_nr]++;
            }
#endif
        }
    if defined BIT_HIST
        if((count>0)&&(iter_nr >= THRESHOLD_ITER))
            bit_hist_block[iter_nr]++;
    #endif
    return (count);
}

/*****
/* print_err() append to the file the nr. of errors and BER */
/* returns: number of bit errors in a block */
int print_err(int *datal, double *data2, int iter_no, int block_no, int *err)
{
    int i, j, nr;
    int block_err = 0;
    char fname[] = BIT_HIST_FILE_NAME;
    char sss[] = {'0','1','2','3','4','5','6','7','8','9'};
    FILE *out_file = NULL;
    int *pi;

    if((iter_no == 1) && (block_no == 1))
    {
        out_file = fopen(ERROR_FILE_NAME, "a");
        if(!out_file)
        {
            printf("Error2: the output file could not be opened!\n");
            exit (1);
        }
        fprintf(out_file, "ref_tc.c, RSC1_enc_mem = %d, RSC1_fp = %d, RSC1_bp = %d,
RSC2_enc_mem = %d, RSC2_fp = %d, RSC2_bp = %d, s1 = %d, s2 = %d, int_size = %d, Limit soft
outputs to = %e, Eb/No = %f dB\n", RSC1_ENC_MEM, RSC1_FP, RSC1_BP, RSC2_ENC_MEM, RSC2_FP,
RSC2_BP, SEED1, SEED2, INT_SIZE, (double) MAX, (double) EBNO);
        fclose(out_file);
    }
    block_err = errors(datal, data2, INT_SIZE, iter_no);
    err[iter_no - 1] += block_err;

    ++frame_hist[(iter_no-1)*(INT_SIZE+1) + block_err];

    if((iter_no == NR_ITER) && (block_err != 0))
        ++frame_err;

```

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```

#if defined BIT_HIST
    if((block_err != 0) && (iter_no >= THRESHOLD_ITER))
    {
        fname[strlen(fname)-1] = sss[iter_no];
        out_file = fopen(fname, "a");
        if(!out_file)
        {
            printf("Error: the bit_hist file could not be opened!\n");
            exit (1);
        }
        for(pi = bit_hist_array[NR_ITER + iter_no]; pi < bit_hist_array[iter_no]; pi = pi+2)
            fprintf(out_file, "\n%06d %06d", *pi, *(pi+1));
        fclose(out_file);
        bit_hist_array[iter_no] = bit_hist_array[NR_ITER + iter_no];
    }
#endif

    if(((iter_no == NR_ITER) && (((block_no % PRINT_BLOCKS) == 0) || (err[NR_ITER - 1] >
MAX_ERRORS))) || (((block_no % PRINT_BLOCKS) == 0) && (block_err == 0)))

    {
        out_file = fopen(ERROR_FILE_NAME, "a");
        if(!out_file)
        {
            printf("Error3: the output file could not be opened!\n");
            exit (1);
        }
        nr = block_no * INT_SIZE;
        fprintf(out_file, "\n\nNr. of info bits:  %d (%d blocks)",
            nr, block_no);
        for(j = 0; j < NR_ITER; j++)
            fprintf(out_file, "\nIter: %02d, Errors: %06d, BER = %e",
                j + 1, err[j], (double)err[j]/INT_SIZE/block_no);
        total_err = err[NR_ITER - 1];
        fprintf(out_file, "\nFrame error = %f(%f errors per block)\n",
            (double)frame_err/block_no,
            (frame_err == 0?0.0:(double)err[NR_ITER-1]/frame_err));
        fclose(out_file);

        if((block_no % 100000) == 0)
        {
            out_file = fopen(FRAME_HIST_FILE_NAME, "a");
            if(!out_file)
            {
                printf("Error4: the .fhist file could not be opened!\n");
                exit (1);
            }
            nr = block_no * INT_SIZE;
            fprintf(out_file, "\n\nNr. of info bits:  %d (%d blocks)",
                nr, block_no);
            for(j = 0; j <= INT_SIZE; j++)
                fprintf(out_file, "\n%03d %03d",
                    j, frame_hist[(NR_ITER-1)*(INT_SIZE+1)+j]);
            fclose(out_file);
        }
    }
return (block_err);
}

/*****
/* This is a MAP decoder for a cs->nr_states states jat_code.          */
/* function:  decodes a block of received data of length INT_SIZE.      */
/*           It assumes that the encoder state starts from state zero   */
/* input:    code structure, I address, Q address, L_in address         */
/* output:   the extrinsic information in L_out                          */
/* globals:  noise                                                        */
*****/

```

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```

/*
*****
* As jat_map but outputs probability and not log(probability)
* It also can handle very large interleavers
*/
void jat_map1(jat_code *cs, double *I, double *Q, double *L_in, double *L_out)
{
    double    sum, sum_0, sum_1, max;
    int       i, j, k, st;
    double    *alpha_old;
    double    *alpha_new;
    double    *beta0;
    double    *betal;
    double    *probI;
    double    *probQ;

    alpha_old = (double *)malloc(sizeof(double) * 2 * cs->nr_states);
    alpha_new = (double *)malloc(sizeof(double) * 2 * cs->nr_states);

    beta0 = (double *)malloc(sizeof(double) * INT_SIZE * cs->nr_states);
    if(beta0 == 0)
    {
        printf("Couldn't allocate beta0 memory!\n");
        exit(1);
    }

    betal = (double *)malloc(sizeof(double) * INT_SIZE * cs->nr_states);
    if(betal == 0)
    {
        printf("Couldn't allocate betal memory!\n");
        exit(1);
    }

    probI = (double *)malloc(sizeof(double) * INT_SIZE);
    if(probI == 0)
    {
        printf("Couldn't allocate probI memory!\n");
        exit(1);
    }

    probQ = (double *)malloc(sizeof(double) * INT_SIZE);
    if(probQ == 0)
    {
        printf("Couldn't allocate probQ memory!\n");
        exit(1);
    }

    /* initialize the alpha_old metrics */
    for(st = 0; st < cs->nr_states; st++)
        for(k = 0; k < 2; k++)
            *(alpha_old + k * cs->nr_states + st) = 0.0;

    *(alpha_old + cs->P0state[0]) = 1.0;
    *(alpha_old + cs->nr_states + cs->P1state[0]) = 1.0;

    /* initialize beta's */
    for(st = 0; st < cs->nr_states; st++)
    {
        beta0[(INT_SIZE - 1) * cs->nr_states + st] = 1.0;
        betal[(INT_SIZE - 1) * cs->nr_states + st] = 1.0;
    }

    /* compute all beta's */
    for(i = INT_SIZE - 2; i >= 0; i--)
    {
        probI[i + 1] = exp(I[i + 1]) * L_in[i + 1];
        probQ[i + 1] = exp(Q[i + 1]);
        for(st = 0; st < cs->nr_states; st++)
        {
            /* compute beta0[i][st]:

```


COMPUTER PROGRAM LISTING APPENDIX

```

        beta0[i * cs->nr_states + st] = beta0[(i + 1) * cs->nr_states + cs-
>N0state[st]]*
        ((cs->Coded0[cs->N0state[st]] == 0)?1:probQ[i + 1])+
        betal[(i + 1) * cs->nr_states + cs->N0state[st]]*probI[i + 1]*
        ((cs->Coded1[cs->N0state[st]] == 0)?1:probQ[i + 1]);
        betal[i * cs->nr_states + st] = beta0[(i + 1) * cs->nr_states + cs-
>N1state[st]]*
        ((cs->Coded0[cs->N1state[st]] == 0)?1:probQ[i + 1])+
        betal[(i + 1) * cs->nr_states + cs->N1state[st]]*probI[i + 1]*
        ((cs->Coded1[cs->N1state[st]] == 0)?1:probQ[i + 1]);
    }

    max = beta0[i * cs->nr_states];
    for(st = 1; st < cs->nr_states; st++)
        if(beta0[i * cs->nr_states + st] > max)
            max = beta0[i * cs->nr_states + st];
    for(st = 0; st < cs->nr_states; st++)
        if(betal[i * cs->nr_states + st] > max)
            max = betal[i * cs->nr_states + st];
    for(st = 0; st < cs->nr_states; st++)
    {
        beta0[i * cs->nr_states + st] = beta0[i * cs->nr_states + st] / max;
        betal[i * cs->nr_states + st] = betal[i * cs->nr_states + st] / max;
    }
}

/* now we have all beta's; we can compute alpha for all states for each */
/* data bit and using beta's we compute lambda */
probI[0] = exp(I[0]) * L_in[0];
probQ[0] = exp(Q[0]);
for(k = 0; k < INT_SIZE; k++)
{
    for(st = 0; st < cs->nr_states; st++)
    {
        sum = *(alpha_old + cs->P0state[st]) + *(alpha_old + cs->nr_states + cs-
>P1state[st]);
        *(alpha_new + st) = sum * ((cs->Coded0[st] == 0)?1:probQ[k]);
        *(alpha_new + cs->nr_states + st) = sum * probI[k] * ((cs->Coded1[st] ==
0)?1:probQ[k]);
    }

    /* find the max value and renormalize alpha's: */
    max = *alpha_new;
    for(st = 0; st < cs->nr_states; st++)
        for(j = 0; j < 2; j++)
            if(*(alpha_new + cs->nr_states * j + st) > max)
                max = *(alpha_new + cs->nr_states * j + st);
    for(st = 0; st < cs->nr_states; st++)
        for(j = 0; j < 2; j++)
            *(alpha_new + cs->nr_states * j + st) = *(alpha_new + cs->nr_states * j + st)/
max;

    /* find sum_0 and sum_1 over all states for L_out: */
    sum_0 = 0.0;
    sum_1 = 0.0;
    for(st = 0; st < cs->nr_states; st++)
    {
        sum_0 += *(alpha_new + st) * beta0[k * cs->nr_states + st];
        sum_1 += *(alpha_new + cs->nr_states + st) * betal[k * cs->nr_states + st];
    }

    /* output the extrinsic information: */
    L_out[k] = (sum_1 / sum_0) / exp(I[k]) / L_in[k];
    if(L_out[k] > MAX)
        L_out[k] = MAX;
    if(L_out[k] < 1/MAX)
        L_out[k] = 1/MAX;

    for(st = 0; st < cs->nr_states; st++)
        for(j = 0; j < 2; j++)/* update alphas */
            *(alpha_old + cs->nr_states * j + st)=*(alpha_new + cs->nr_states * j + st);
}

```

```

    }
    free(beta0);
    free(beta1);
    free(probI);
    free(probQ);
    free(alpha_old);
    free(alpha_new);
}

```

```

double find_tx_I(int k)
{
    double tx_I;
    switch(k)
    {
        case 0:
            tx_I = 0.5;
            break;
        case 1:
            tx_I = -3.5;
            break;
        case 2:
            tx_I = 0.5;
            break;
        case 3:
            tx_I = -3.5;
            break;
        case 4:
            tx_I = 2.5;
            break;
        case 5:
            tx_I = -1.5;
            break;
        case 6:
            tx_I = 2.5;
            break;
        case 7:
            tx_I = -1.5;
            break;
        case 8:
            tx_I = 2.5;
            break;
        case 9:
            tx_I = -1.5;
            break;
        case 10:
            tx_I = 2.5;
            break;
        case 11:
            tx_I = -1.5;
            break;
        case 12:
            tx_I = 0.5;
            break;
        case 13:
            tx_I = -3.5;
            break;
        case 14:
            tx_I = 0.5;
            break;
        case 15:
            tx_I = -3.5;
            break;
        case 16:
            tx_I = 1.5;
            break;
        case 17:
            tx_I = -2.5;
            break;
    }
}

```

COMPUTER PROGRAM LISTING APPENDIX

```
case 18:
    tx_I = 1.5;
    break;
case 19:
    tx_I = -2.5;
    break;
case 20:
    tx_I = 3.5;
    break;
case 21:
    tx_I = -0.5;
    break;
case 22:
    tx_I = 3.5;
    break;
case 23:
    tx_I = -0.5;
    break;
case 24:
    tx_I = 3.5;
    break;
case 25:
    tx_I = -0.5;
    break;
case 26:
    tx_I = 3.5;
    break;
case 27:
    tx_I = -0.5;
    break;
case 28:
    tx_I = 1.5;
    break;
case 29:
    tx_I = -2.5;
    break;
case 30:
    tx_I = 1.5;
    break;
case 31:
    tx_I = -2.5;
    break;
case 32:
    tx_I = 1.5;
    break;
case 33:
    tx_I = -2.5;
    break;
case 34:
    tx_I = 1.5;
    break;
case 35:
    tx_I = -2.5;
    break;
case 36:
    tx_I = 3.5;
    break;
case 37:
    tx_I = -0.5;
    break;
case 38:
    tx_I = 3.5;
    break;
case 39:
    tx_I = -0.5;
    break;
case 40:
    tx_I = 3.5;
    break;
case 41:
    tx_I = -0.5;
```

COMPUTER PROGRAM LISTING APPENDIX

```

        break;
    case 42:
        tx_I = 3.5;
        break;
    case 43:
        tx_I = -0.5;
        break;
    case 44:
        tx_I = 1.5;
        break;
    case 45:
        tx_I = -2.5;
        break;
    case 46:
        tx_I = 1.5;
        break;
    case 47:
        tx_I = -2.5;
        break;
    case 48:
        tx_I = 0.5;
        break;
    case 49:
        tx_I = -3.5;
        break;
    case 50:
        tx_I = 0.5;
        break;
    case 51:
        tx_I = -3.5;
        break;
    case 52:
        tx_I = 2.5;
        break;
    case 53:
        tx_I = -1.5;
        break;
    case 54:
        tx_I = 2.5;
        break;
    case 55:
        tx_I = -1.5;
        break;
    case 56:
        tx_I = 2.5;
        break;
    case 57:
        tx_I = -1.5;
        break;
    case 58:
        tx_I = 2.5;
        break;
    case 59:
        tx_I = -1.5;
        break;
    case 60:
        tx_I = 0.5;
        break;
    case 61:
        tx_I = -3.5;
        break;
    case 62:
        tx_I = 0.5;
        break;
    case 63:
        tx_I = -3.5;
        break;
    }
    return(tx_I);
}

```

COMPUTER PROGRAM LISTING APPENDIX

```
double find_tx_Q(int k)
{
    double tx_Q;
    switch(k)
    {
        case 0:
            tx_Q = 2.5;
            break;
        case 1:
            tx_Q = 2.5;
            break;
        case 2:
            tx_Q = -1.5;
            break;
        case 3:
            tx_Q = -1.5;
            break;
        case 4:
            tx_Q = 0.5;
            break;
        case 5:
            tx_Q = 0.5;
            break;
        case 6:
            tx_Q = -3.5;
            break;
        case 7:
            tx_Q = -3.5;
            break;
        case 8:
            tx_Q = 2.5;
            break;
        case 9:
            tx_Q = 2.5;
            break;
        case 10:
            tx_Q = -1.5;
            break;
        case 11:
            tx_Q = -1.5;
            break;
        case 12:
            tx_Q = 0.5;
            break;
        case 13:
            tx_Q = 0.5;
            break;
        case 14:
            tx_Q = -3.5;
            break;
        case 15:
            tx_Q = -3.5;
            break;
        case 16:
            tx_Q = 3.5;
            break;
        case 17:
            tx_Q = 3.5;
            break;
        case 18:
            tx_Q = -0.5;
            break;
        case 19:
            tx_Q = -0.5;
            break;
        case 20:
            tx_Q = 1.5;
            break;
        case 21:
            tx_Q = 1.5;
    }
}
```

COMPUTER PROGRAM LISTING APPENDIX

```

        break;
case 22:
    tx_Q = -2.5;
    break;
case 23:
    tx_Q = -2.5;
    break;
case 24:
    tx_Q = 3.5;
    break;
case 25:
    tx_Q = 3.5;
    break;
case 26:
    tx_Q = -0.5;
    break;
case 27:
    tx_Q = -0.5;
    break;
case 28:
    tx_Q = 1.5;
    break;
case 29:
    tx_Q = 1.5;
    break;
case 30:
    tx_Q = -2.5;
    break;
case 31:
    tx_Q = -2.5;
    break;
case 32:
    tx_Q = 2.5;
    break;
case 33:
    tx_Q = 2.5;
    break;
case 34:
    tx_Q = -1.5;
    break;
case 35:
    tx_Q = -1.5;
    break;
case 36:
    tx_Q = 0.5;
    break;
case 37:
    tx_Q = 0.5;
    break;
case 38:
    tx_Q = -3.5;
    break;
case 39:
    tx_Q = -3.5;
    break;
case 40:
    tx_Q = 2.5;
    break;
case 41:
    tx_Q = 2.5;
    break;
case 42:
    tx_Q = -1.5;
    break;
case 43:
    tx_Q = -1.5;
    break;
case 44:
    tx_Q = 0.5;
    break;
case 45:

```

COMPUTER PROGRAM LISTING APPENDIX

```

        tx_Q = 0.5;
        break;
    case 46:
        tx_Q = -3.5;
        break;
    case 47:
        tx_Q = -3.5;
        break;
    case 48:
        tx_Q = 3.5;
        break;
    case 49:
        tx_Q = 3.5;
        break;
    case 50:
        tx_Q = -0.5;
        break;
    case 51:
        tx_Q = -0.5;
        break;
    case 52:
        tx_Q = 1.5;
        break;
    case 53:
        tx_Q = 1.5;
        break;
    case 54:
        tx_Q = -2.5;
        break;
    case 55:
        tx_Q = -2.5;
        break;
    case 56:
        tx_Q = 3.5;
        break;
    case 57:
        tx_Q = 3.5;
        break;
    case 58:
        tx_Q = -0.5;
        break;
    case 59:
        tx_Q = -0.5;
        break;
    case 60:
        tx_Q = 1.5;
        break;
    case 61:
        tx_Q = 1.5;
        break;
    case 62:
        tx_Q = -2.5;
        break;
    case 63:
        tx_Q = -2.5;
        break;
    }
    return(tx_Q);
}

```

```

/*****
/* This is a MAP decoder for a cs->nr_states states jat_code. */
/* function: decodes a block of received data of length INT_SIZE/2. */
/*           It assumes that the encoder state starts from state zero */
/* input:    code structure, I address, Q address, L_in address */
/* output:   the extrinsic information in L_out */
/* globals:  noise */

```

```

/*

```

COMPUTER PROGRAM LISTING APPENDIX

```

*****
* As jat_map but outputs probability and not log(probability)
* It also can handle very large interleavers
*/
void jat_map2(jat_code *cs, double *I, double *Q, double *L_in, double *L_out)
{
    double    sum, sum_0, sum_1, max;
    int       i, j, k, st;
    double    *alpha_old;
    double    *alpha_new;
    double    *beta0;
    double    *betal;
    double    *probI;
    double    *probQ;

    alpha_old = (double *)malloc(sizeof(double) * 2 * cs->nr_states);
    alpha_new = (double *)malloc(sizeof(double) * 2 * cs->nr_states);

    beta0 = (double *)malloc(sizeof(double) * INT_SIZE/2 * cs->nr_states);
    if(beta0 == 0)
    {
        printf("Couldn't allocate beta0 memory!\n");
        exit(1);
    }

    betal = (double *)malloc(sizeof(double) * INT_SIZE/2 * cs->nr_states);
    if(betal == 0)
    {
        printf("Couldn't allocate betal memory!\n");
        exit(1);
    }

    probI = (double *)malloc(sizeof(double) * INT_SIZE/2);
    if(probI == 0)
    {
        printf("Couldn't allocate probI memory!\n");
        exit(1);
    }

    probQ = (double *)malloc(sizeof(double) * INT_SIZE/2);
    if(probQ == 0)
    {
        printf("Couldn't allocate probQ memory!\n");
        exit(1);
    }

    /* initialize the alpha_old metrics */
    for(st = 0; st < cs->nr_states; st++)
        for(k = 0; k < 2; k++)
            *(alpha_old + k * cs->nr_states + st) = 0.0;

    *(alpha_old + cs->P0state[0]) = 1.0;
    *(alpha_old + cs->nr_states + cs->P1state[0]) = 1.0;

    /* initialize beta's */
    for(st = 0; st < cs->nr_states; st++)
    {
        beta0[(INT_SIZE/2 - 1) * cs->nr_states + st] = 1.0;
        betal[(INT_SIZE/2 - 1) * cs->nr_states + st] = 1.0;
    }

    /* compute all beta's */
    for(i = INT_SIZE/2 - 2; i >= 0; i--)
    {
        probI[i + 1] = exp(I[i + 1]) * L_in[i + 1];
        probQ[i + 1] = exp(Q[i + 1]);
        for(st = 0; st < cs->nr_states; st++)
        {
            /* compute beta0[i][st]:

```


COMPUTER PROGRAM LISTING APPENDIX

```

        beta0[i * cs->nr_states + st] = beta0[(i + 1) * cs->nr_states + cs-
>N0state[st]]*
            ((cs->Coded0[cs->N0state[st]] == 0)?1:probQ[i + 1])+
            betal[(i + 1) * cs->nr_states + cs->N0state[st]]*probI[i + 1]*
            ((cs->Coded1[cs->N0state[st]] == 0)?1:probQ[i + 1]);
        betal[i * cs->nr_states + st] = beta0[(i + 1) * cs->nr_states + cs-
>N1state[st]]*
            ((cs->Coded0[cs->N1state[st]] == 0)?1:probQ[i + 1])+
            betal[(i + 1) * cs->nr_states + cs->N1state[st]]*probI[i + 1]*
            ((cs->Coded1[cs->N1state[st]] == 0)?1:probQ[i + 1]);
    }

    max = beta0[i * cs->nr_states];
    for(st = 1; st < cs->nr_states; st++)
        if(beta0[i * cs->nr_states + st] > max)
            max = beta0[i * cs->nr_states + st];
    for(st = 0; st < cs->nr_states; st++)
        if(betal[i * cs->nr_states + st] > max)
            max = betal[i * cs->nr_states + st];
    for(st = 0; st < cs->nr_states; st++)
    {
        beta0[i * cs->nr_states + st] = beta0[i * cs->nr_states + st] / max;
        betal[i * cs->nr_states + st] = betal[i * cs->nr_states + st] / max;
    }
}

/* now we have all beta's; we can compute alpha for all states for each */
/* data bit and using beta's we compute lambda */
probI[0] = exp(I[0]) * L_in[0];
probQ[0] = exp(Q[0]);
for(k = 0; k < INT_SIZE/2; k++)
{
    for(st = 0; st < cs->nr_states; st++)
    {
        sum = *(alpha_old + cs->P0state[st]) + *(alpha_old + cs->nr_states + cs-
>P1state[st]);
        *(alpha_new + st) = sum * ((cs->Coded0[st] == 0)?1:probQ[k]);
        *(alpha_new + cs->nr_states + st) = sum * probI[k] * ((cs->Coded1[st] ==
0)?1:probQ[k]);
    }
}

/* find the max value and renormalize alpha's: */
max = *alpha_new;
for(st = 0; st < cs->nr_states; st++)
    for(j = 0; j < 2; j++)
        if(*(alpha_new + cs->nr_states * j + st) > max)
            max = *(alpha_new + cs->nr_states * j + st);
for(st = 0; st < cs->nr_states; st++)
    for(j = 0; j < 2; j++)
        *(alpha_new + cs->nr_states * j + st) = *(alpha_new + cs->nr_states * j + st)/
max;

/* find sum_0 and sum_1 over all states for L_out: */
sum_0 = 0.0;
sum_1 = 0.0;
for(st = 0; st < cs->nr_states; st++)
{
    sum_0 += *(alpha_new + st) * beta0[k * cs->nr_states + st];
    sum_1 += *(alpha_new + cs->nr_states + st) * betal[k * cs->nr_states + st];
}

/* output the extrinsic information: */
L_out[k] = (sum_1 / sum_0) / exp(I[k]) / L_in[k];
if(L_out[k] > MAX)
    L_out[k] = MAX;
if(L_out[k] < 1/MAX)
    L_out[k] = 1/MAX;

for(st = 0; st < cs->nr_states; st++)
    for(j = 0; j < 2; j++)/* update alphas */
        *(alpha_old + cs->nr_states * j + st)=*(alpha_new + cs->nr_states * j + st);

```

COMPUTER PROGRAM LISTING APPENDIX

```
    }  
    free(beta0);  
    free(beta1);  
    free(probI);  
    free(probQ);  
    free(alpha_old);  
    free(alpha_new);  
}
```

COMPUTER PROGRAM LISTING APPENDIX

interlever.c

```

#define MAX_CINDEX 46
#define MAX_RINDEX 47
#define MAX_ELEMENT 2100
#include <stdio.h>
#include <stdlib.h>

void main (void)
{
    int ra, ca; //Ia sequence row and column indices
    int count; //Counter for each bit in DMT frame
    int element; //Element number used for finding if element within array
    FILE *output;

    output=fopen("interleaver","w");
    //Initial sequence indices

    ra=MAX_RINDEX-1;
    ca=0;

    //Adjust the initial indices for Ia if beyond ending element
    element=ra*MAX_CINDEX+ca;

    while (element >=MAX_ELEMENT) {
        ra--;
        ca++;
        if (ra<0) {
            ra=MAX_RINDEX-1;
            ca=ca+(MAX_RINDEX-1);
        }
        ca=ca%MAX_CINDEX;

        element= ra*MAX_CINDEX+ca;
    }

    //Fetch all elements in sequence Ia
    for (count = 0; count<MAX_ELEMENT; count++) {
        //Fetch array[ra][ca]
        element=ra*MAX_CINDEX+ca;
        fprintf(output,"%d %d\n",count,element);
        //Update indices for next access

        do {
            ra--;
            ca++;
            if (ra<0) {
                ra=MAX_RINDEX-1;
                ca=ca+(MAX_RINDEX-1);
            }
            ca=ca%MAX_CINDEX;

            element = ra * MAX_CINDEX+ca;
        } while (element >= MAX_ELEMENT);
    }
}

```

COMPUTER PROGRAM LISTING APPENDIX

S-type interleaver generator

```

program int(input,output);
{This program generates mod-k S-random and symmetric mod-k S-random interleavers.

const Nmax = 65536; {maximum interleaver size}

var G,H,I,J,K,L,M,N,S,count,temp,prt,i_,j_,k_,im,jm:longint;
    inta,hat,deint:array[0..Nmax] of longint;
    pass,good:boolean;
    s1,s2:longint; {seeds for function uniform}
    into,deinto:text;
    sym:char;

function max(x,y:longint):longint;
{Finds the maximum of x and y}
begin{max}
    if x > y
    then max := x
    else max := y;
end;{max}

function min(x,y:longint):longint;
{Finds the maximum of x and y}
begin{min}
    if x < y
    then min := x
    else min := y;
end;{min}

function uniform(var s1,s2:longint):double;
{Generates a random number from 0.0 < x < 1.0}
const m0 = 2147483562;
      m1 = 2147483563;
      m2 = 2147483399;
      a1 = 40014;
      a2 = 40692;
      q1 = 53668;
      q2 = 52774;
      r1 = 12211;
      r2 = 3791;
var k:longint;
begin{uniform}
    k := s1 div q1;
    s1 := a1*(s1-k*q1) - k*r1;
    if s1 < 0 then s1 := s1+m1;

    k := s2 div q2;
    s2 := a2*(s2-k*q2) - k*r2;
    if s2 < 0 then s2 := s2+m2;

    k := s1-s2;
    if k < 1 then k := k+m0;
    uniform := k/m1;
end;{uniform}

procedure srandom;
{Generates mod-k S-random interleaver}
label 98;

procedure reject;
{reject random number}
begin{reject}
    count := count-1;
    if count = 0
    then begin{bad int}
        good := false;
        goto 98;
    end;{bad int}

```

COMPUTER PROGRAM LISTING APPENDIX

```

pass := false;
for M := K to count-1 do
  hat[M] := hat[M+1];
  hat[count] := J;
end; {reject}

begin {S-random}
  repeat
    writeln('seed1 = ', s1:1, ', seed2 = ', s2:1);
    good := true;
    for I := 0 to N-1 do
      hat[I] := I;
    for I := 0 to N-1 do
      begin {make int}
        count := N-I;
        i_ := I mod k_;
        im := min(i_, k_-i_);
        repeat
          pass := true;
          K := trunc(count*uniform(s1,s2));
          if K = count then K := K-1;
          J := hat[K];
          if k_ > 1 then
            begin {mod k test}
              j_ := J mod k_;
              jm := min(j_, k_-j_);
              if im <> jm then reject;
            end; {mod k test}
          if pass = true then
            begin {S-random test}
              for L := max(0, I-S) to I-1 do
                if (abs(J-inta[L]) <= S) and (pass = true) then reject;
            end; {S-random test}
          until pass = true;
          for M := K to N-I-2 do
            hat[M] := hat[M+1];
            inta[I] := J;
          end; {make int}
        until good = true;
      end; {S-random};

procedure trandom;
{Generates symmetric mod-k S-random interleaver}
label 99;

procedure rejectS;
{reject random number}
begin {reject S}
  count := count-1;
  if count = 0 then
    begin {bad int}
      good := false;
      goto 99;
    end; {bad int}
  pass := false;
  inta[I] := -1;
  inta[J] := -1;
  for M := K to count-1 do
    hat[M] := hat[M+1];
  hat[count] := J;
end; {reject S}

procedure test;
{S-random test}
begin {test}
  if (inta[L] >= 0) and (abs(G-inta[L]) <= S) then rejectS;
  L := L+1;
end; {test}

begin {T-random}

```

COMPUTER PROGRAM LISTING APPENDIX

```

repeat
  writeln('seed1 = ',s1:1,', seed2 = ',s2:1);
  good := true;
  for I := 0 to N-1 do
    begin{init}
      hat[I] := I;
      inta[I] := -1;
    end;{init}
  H := N;
  I := 0;
  repeat
    count := H;
    while (inta[I] >= 0) and (I < N) do I := I+1;
    i_ := I mod k_;
    im := min(i_,k_-i_);
    repeat
      pass := true;
      K := trunc(count*uniform(s1,s2));
      if K = count then K := K-1;
      J := hat[K];
      if k_ > 1 then
        begin{mod k test}
          j_ := J mod k_;
          jm := min(j_,k_-j_);
          if im <> jm then rejectS;
        end;{mod k test}
      if pass = true then
        begin{S-random test}
          inta[I] := J;
          inta[J] := I;
          G := J;
          L := max(0,I-S);
          while (pass = true) and (L < I) do test;
          L := I+1;
          while (pass = true) and (L < min(I+S,N)) do test;
          G := I;
          L := max(0,J-S);
          while (pass = true) and (L < J) do test;
          L := J+1;
          while (pass = true) and (L < min(J+S,N)) do test;
        end;{S-random test}
      until pass = true;

      H := H-1;
      for M := K to H-1 do
        hat[M] := hat[M+1];
      if I <> J then
        begin{sym}
          K := 0;
          while (hat[K] <> I) and (K < H) do K := K+1;
          H := H-1;
          for M := K to H-1 do
            hat[M] := hat[M+1];
          end;{sym}
        until H = 0;
      99:
    until good = true;
  end{T-random};

begin{int}
  s1 := 12345; {initialise seeds for uniform}
  s2 := 67890;

  writeln;
  writeln('Random Interleaver Generator V1.01');
  writeln('Copyright (c) 1998 Small World Communications. All rights reserved.');
```

COMPUTER PROGRAM LISTING APPENDIX

```

write('Enter mod-k parameter (k=1 is normal): ');
readln(k_);
repeat
  write('Do you want a symmetric interleaver? ');
  readln(sym);
  pass := (sym = 'y') or (sym = 'Y') or (sym = 'n') or (sym = 'N');
  if pass = false then
    writeln('Invalid entry. Try again.');
```

until pass = true;

```

writeln;
case sym of
  'y','Y': trandom;
  'n','N': srandom;
end;{case}

assign(into,'int.dat');
rewrite(into);
for I := 0 to N-1 do
  writeln(into,inta[I]:1);
close(into);

for I := 0 to N-1 do
  hat[I] := 0;
for I := 0 to N-1 do
  begin{test}
    J := inta[I];
    hat[J] := hat[J] + 1;
  end;{test}
pass := true;
for I := 0 to N-1 do
  if hat[I] < 1 then pass := false;
if pass = false
  then writeln('Bad interleaver!');
```

pass := true;

```

I := 0;
repeat
  J := inta[I];
  for L := max(0,I-S) to I-1 do
    if (abs(J-inta[L]) <= S) and (pass = true)
      then begin
        pass := false;
        writeln('Interleaver failed S-test');
        writeln(I:1,' ',inta[I]:1,' ',L:1,' ',inta[L]:1);
      end;
  I := I+1;
until (pass = false) or (I = N);

K := 0;
for I := 0 to N-1 do
  K := max(K,abs(I-inta[I]));
writeln('Dmin = ',K:1);
writeln('Interleaver table int.dat succussfully generated');
```

end.{int}